

Tracking of Multiple Targets Using Online Learning for Reference Model Adaptation

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Abstract—Recently, much work has been done in multiple object tracking on the one hand and on reference model adaptation for a single-object tracker on the other side. In this paper, we do both tracking of multiple objects (faces of people) in a meeting scenario and online learning to incrementally update the models of the tracked objects to account for appearance changes during tracking. Additionally, we automatically initialize and terminate tracking of individual objects based on low-level features, i.e., face color, face size, and object movement. Many methods unlike our approach assume that the target region has been initialized by hand in the first frame. For tracking, a particle filter is incorporated to propagate sample distributions over time. We discuss the close relationship between our implemented tracker based on particle filters and genetic algorithms. Numerous experiments on meeting data demonstrate the capabilities of our tracking approach. Additionally, we provide an empirical verification of the reference model learning during tracking of indoor and outdoor scenes which supports a more robust tracking. Therefore, we report the average of the standard deviation of the trajectories over numerous tracking runs depending on the learning rate.

Index Terms—Genetic algorithms (GAs), multiple target tracking, particle filter, reference model learning, visual tracking.

I. INTRODUCTION

VISUAL tracking of multiple objects is concerned with maintaining the correct identity and location of a variable number of objects over time irrespective of occlusions and visual alterations. Lim *et al.* [1] differentiate between intrinsic and extrinsic appearance variability including pose variation, shape deformation of the object and illumination change, camera movement, occlusions, respectively.

In the past few years, particle filters have become the method of choice for tracking. Isard and Blake [2] introduced particle filtering (condensation algorithm). Many different sampling schemes have been suggested in the meantime. An overview about sampling schemes of particle filters and the relation to Kalman filters is provided in [3].

Recently, the main emphasis is on simultaneously tracking multiple objects and on online learning to adapt the reference models to the appearance changes, e.g., pose variation, illumination change. Lim *et al.* [1] introduce a single-object tracker, where the target representation—a low-dimensional eigenspace representation—is incrementally updated to model the appear-

ance variability. They assume, like most tracking algorithms, that the target region is initialized by hand in the first frame. Jepson *et al.* [4] use a Gaussian mixture model which is adapted using an online expectation maximization (EM) algorithm to account for appearance changes. Their WSL tracker uses a wavelet-based object model which is useful for tracking objects where regions of the objects (i.e., faces) are stable while other regions vary, e.g., mouth. McKenna *et al.* [5] employ Gaussian mixtures of the color distributions of the objects as adaptive model. In [6], simple color histograms are used to represent the objects (similar as in [7]). However, they introduce a simple update of the histograms to overcome the appearance changes of the object. All the aforementioned articles are focused on tracking a single object. For tracking multiple objects, most algorithms belong to one of the following three categories: 1) Multiple instances of a single-object tracker are used [8]. 2) All objects of interest are included in the state space [9]. A fixed number of objects is assumed. Varying number of objects result in a dynamic change of the dimension of the state space. 3) Most recently, the framework of particle filters is extended to capture multiple targets using a mixture model [10]. This mixture particle filter—where each component models an individual object—enables interaction between the components by the importance weights. In [11], this approach is extended by the Adaboost algorithm to learn the models of the targets. The information from Adaboost enables detection of objects entering the scene automatically. The mixture particle filter is further extended in [12] to handle mutual occlusions. They introduce a rectification technique to compensate for camera motions, a global nearest neighbor data association method to correctly identify object detections with existing tracks, and a mean-shift algorithm which accounts for more stable trajectories for reliable motion prediction.

In this paper, we do both tracking of multiple persons in a meeting scenario and online adaptation of the models to account for appearance changes during tracking. The tracking is based on low-level features such as skin color, object motion, and object size. Based on these features, automatic initialization and termination of objects are performed. The aim is to use as little prior knowledge as possible. For tracking, a particle filter is incorporated to propagate sample distributions over time. Our implementation is related to the *dual estimation* problem [13], where both the states of multiple objects and the parameters of the reference models are simultaneously estimated given the observations. At every time step, the particle filter estimates the states using the observation likelihood of the current reference models while the online learning of the reference models is based on the current state estimates. Additionally, we discuss

Manuscript received July 24, 2007; revised January 30, 2008. This work was supported by the Austrian Science Fund under Project P19737-N15.

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Digital Object Identifier 10.1109/TSMCB.2008.927281

94 the similarity between our implemented tracker based on parti-
 95 cle filters and genetic algorithms (GAs). We want to emphasize
 96 this close connection since approaches what have indepen-
 97 dently been developed in one community might turn out to be
 98 very useful for the other community and vice versa. Numerous
 99 experiments on meeting data demonstrate the capabilities of our
 100 tracking approach. Additionally, we empirically show that the
 101 adaptation of the reference model during tracking of an indoor
 102 and outdoor scenes results in a more robust tracking. For this,
 103 we report the average of the standard deviation of the trajecto-
 104 ries over numerous independent tracking runs depending on the
 105 learning rate.

106 The proposed approach differs from previous methods in
 107 several aspects. Recently, much work has been done in multiple
 108 object tracking on the one hand side and on reference model
 109 adaptation for a single-object tracker on the other side. In this
 110 paper, we do both tracking of multiple objects and online learn-
 111 ing to incrementally update the representation of the tracked ob-
 112 jects to model appearance changes. We use the Jensen–Shannon
 113 (JS) divergence [14] to measure the similarity between the
 114 tracked object and its reference model. Additionally, we discuss
 115 its advantages compared to the Kullback–Leibler divergence
 116 [15] and the Bhattacharyya similarity coefficient [16]. We auto-
 117 matically initialize and terminate tracking of individual objects
 118 based on low-level features, i.e., face color, face size, and object
 119 movement. Many methods unlike our approach assume that the
 120 target region has been initialized in the first frame.

121 This paper is organized as follows. Section II introduces
 122 the particle filter for multiple object tracking, the state-space
 123 dynamics, the observation model, automatic initialization and
 124 termination of objects, and the online learning of the mod-
 125 els for the tracked objects. Section II-G summarizes the im-
 126 plemented tracker on the basis of pseudocode. Section III
 127 sketches the relationship to GA. The tracking results on a
 128 meeting scenario and for indoor/outdoor scenes are presented in
 129 Section IV. Additionally, we provide empirical verification of
 130 the reference model learning in this section. Section V con-
 131 cludes this paper.

132 II. TRACKING USING PARTICLE FILTERS

133 In many applications the states of a dynamic system have
 134 to be estimated from a time series of noisy observations. The
 135 Kalman filter [13], [17] is a linear dynamical system [18] that
 136 provides a linear time-discrete filter that estimates the states
 137 online over time once observations become available. This
 138 filter is recursive in a sense that each current state estimate
 139 is computed from the previous estimate and the current ob-
 140 served data. In contrast to linear dynamical systems, the hidden
 141 Markov model [19] assumes a discrete state space. Recently,
 142 many extensions of the basic linear dynamical system have
 143 been proposed [13] to overcome the assumption of the linear-
 144 Gaussian model used for the observations and state transition,
 145 e.g., the extended Kalman filter, unscented Kalman filter, or
 146 the switching state-space model [20]. Another approach for
 147 filtering is to use sequential Monte Carlo methods which are
 148 also known as particle filters [21]. They are capable to deal with
 149 any nonlinearity or distribution.

A. Particle Filter

150

A particle filter is capable to deal with nonlinear non- 151
 Gaussian processes and has become popular for visual tracking. 152
 For tracking, the probability distribution that the object is in 153
 state \mathbf{x}_t at time t given the observations $\mathbf{y}_{0:t}$ up to time t is of 154
 interest. Hence, $p(\mathbf{x}_t|\mathbf{y}_{0:t})$ has to be constructed starting from 155
 the initial distribution $p(\mathbf{x}_0|\mathbf{y}_0) = p(\mathbf{x}_0)$. In Bayesian filtering, 156
 this can be formulated as iterative recursive process consisting 157
 of the prediction step 158

$$p(\mathbf{x}_t|\mathbf{y}_{0:t-1}) = \int p(\mathbf{x}_t|\mathbf{x}_{t-1})p(\mathbf{x}_{t-1}|\mathbf{y}_{0:t-1})d\mathbf{x}_{t-1} \quad (1)$$

and of the filtering step 159

$$p(\mathbf{x}_t|\mathbf{y}_{0:t}) = \frac{p(\mathbf{y}_t|\mathbf{x}_t)p(\mathbf{x}_t|\mathbf{y}_{0:t-1})}{\int p(\mathbf{y}_t|\mathbf{x}_t)p(\mathbf{x}_t|\mathbf{y}_{0:t-1})d\mathbf{x}_t} \quad (2)$$

where $p(\mathbf{x}_t|\mathbf{x}_{t-1})$ is the dynamic model describing the state- 160
 space evolution which corresponds to the evolution of the 161
 tracked object (see Section II-B) and $p(\mathbf{y}_t|\mathbf{x}_t)$ is the likelihood 162
 of an observation \mathbf{y}_t given the state \mathbf{x}_t (see observation model 163
 in Section II-C). 164

In particle filters $p(\mathbf{x}_t|\mathbf{y}_{0:t})$ of the filtering step is ap- 165
 proximated by a finite set of weighted samples, i.e., the 166
 particles, $\{\mathbf{x}_t^m, w_t^m\}_{m=1}^M$, where M is the number of sam- 167
 ples. Particles are sampled from a proposal distribution $\mathbf{x}_t^m \sim$ 168
 $q(\mathbf{x}_t|\mathbf{x}_{t-1}, \mathbf{y}_{0:t})$ (importance sampling) [3]. In each iteration, 169
 the importance weights are updated according to 170

$$w_t^m \propto \frac{p(\mathbf{y}_t|\mathbf{x}_t^m)p(\mathbf{x}_t^m|\mathbf{x}_{t-1}^m)}{q(\mathbf{x}_t^m|\mathbf{x}_{t-1}^m, \mathbf{y}_{0:t})} w_{t-1}^m \sum_{m=1}^M w_t^m = 1. \quad (3)$$

One simple choice for the proposal distribution is to take the 171
 prior density $q(\mathbf{x}_t^m|\mathbf{x}_{t-1}^m, \mathbf{y}_{0:t}) = p(\mathbf{x}_t^m|\mathbf{x}_{t-1}^m)$ (bootstrap filter). 172
 Hence, the weights are proportional to the likelihood model 173
 $p(\mathbf{y}_t|\mathbf{x}_t^m)$ 174

$$w_t^m \propto p(\mathbf{y}_t|\mathbf{x}_t^m) w_{t-1}^m. \quad (4)$$

The posterior filtered density $p(\mathbf{x}_t|\mathbf{y}_{1:t})$ can be approx- 175
 imated as 176

$$p(\mathbf{x}_t|\mathbf{y}_{1:t}) \approx \sum_{m=1}^M w_t^m \delta(\mathbf{x}_t - \mathbf{x}_t^m) \quad (5)$$

where $\delta(\mathbf{x}_t - \mathbf{x}_t^m)$ is the Dirac delta function with mass at \mathbf{x}_t^m . 177

We use resampling to reduce the *degeneracy problem* [3], 178
 [21]. We resample the particles $\{\mathbf{x}_t^m\}_{m=1}^M$ with replacement M 179
 times according to their weights w_t^m . The resulting particles 180
 $\{\mathbf{x}_t^m\}_{m=1}^M$ have uniformly distributed weights $w_t^m = 1/M$. 181
 Similar to the sampling importance resampling filter [3], we 182
 resample in every time step. This simplifies (4) to $w_t^m \propto$ 183
 $p(\mathbf{y}_t|\mathbf{x}_t^m)$ since $w_{t-1}^m = 1/M \quad \forall m$. 184

In the meeting scenario, we are interested in tracking the 185
 faces of multiple people. We treat the tracking of multiple 186
 objects completely independent, i.e., we assign a set of M 187
 particles to each tracked object k as $\{\{\mathbf{x}_t^{m,k}\}_{m=1}^M\}_{k=1}^K$, where 188
 K is the total number of tracked objects which dynamically 189

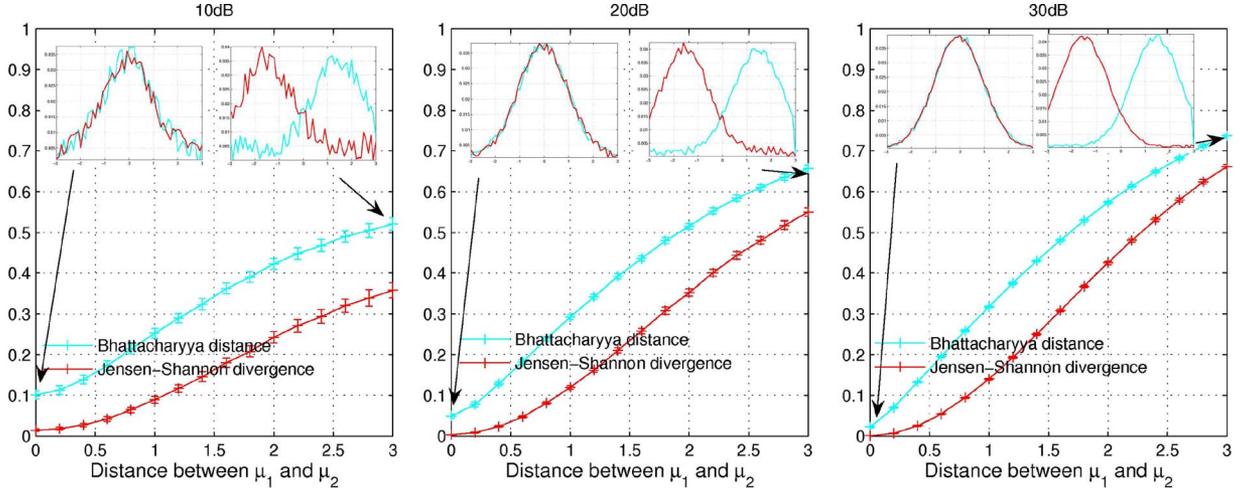


Fig. 1. JS divergence and Bhattacharyya similarity coefficient between two distributions estimated from samples. We added noise at a level of 10, 20, and 30 dB to the distributions.

190 changes over time. Hence, we use multiple instances of a single-
191 object tracker similar to [8].

192 B. State-Space Dynamics

193 The state sequence evolution $\{\mathbf{x}_t; t \in \mathbb{N}\}$ is assumed to be
194 a second-order autoregressive process which is used instead
195 of the first-order formalism ($p(\mathbf{x}_t|\mathbf{x}_{t-1})$) introduced in the
196 previous section. The second-order dynamics can be written as
197 first order by extending the state vector at time t with elements
198 from the state vector at time $t-1$.

199 We define the state vector at time t as $\mathbf{x}_t = [x_t \ y_t \ s_t^x \ s_t^y]^T$.
200 The location of the target at t is given as x_t, y_t , respectively,
201 and s_t^x, s_t^y denote the scale of the tracked region in the $x \times y$
202 image space. In our tracking approach, the transition model
203 corresponds to

$$\mathbf{x}_{t+1}^{m,k} = \mathbf{x}_t^{m,k} + C\mathbf{v}_t + \frac{D}{2M} \sum_{m'=1}^M (\mathbf{x}_t^{m',k} - \mathbf{x}_{t-1}^{m',k}) \quad (6)$$

204 where $\mathbf{v}_t \sim \mathcal{N}(0, \mathbf{I})$ is a simple Gaussian random noise model
205 and the term $1/2M \sum_{m'=1}^M (\mathbf{x}_t^{m',k} - \mathbf{x}_{t-1}^{m',k})$ captures the linear
206 evolution of object k from the particles of the previous time
207 step. Factor D models the influence of the linear evolution,
208 e.g., D is set to 0.5. The parameters of the random noise
209 model are set to $C = \text{diag}([10 \ 10 \ 0.03 \ 0.03])$ with the
210 units of [pixel/frame], [pixel/frame], [1/frame], and [1/frame],
211 respectively.

212 C. Observation Model

213 The shape of the tracked region is determined to be an ellipse
214 [4] since the tracking is focused on the faces of the individuals.
215 We assume that the principal axes of the ellipses are aligned
216 with the coordinate axes of the image. Similarly to [7], we use
217 the color histograms for modeling the target regions. Therefore,
218 we transform the image into the hue-saturation-value (HSV)
219 space [22]. For the sake of readability, we abuse the notation
220 and write the particle $\mathbf{x}_t^{m,k}$ as \mathbf{x}_t in this section. We build
221 an individual histogram for hue (H) $h_H^{\mathbf{x}_t}$, saturation (S) $h_S^{\mathbf{x}_t}$,

and value (V) $h_V^{\mathbf{x}_t}$ of the elliptic candidate region at \mathbf{x}_t . The 222
length of the principal axes of the ellipse are $A_{\text{ref}}^k s_t^x$ and $B_{\text{ref}}^k s_t^y$, 223
respectively, where A_{ref}^k and B_{ref}^k are the length of the ellipse 224
axes of the reference model of object k . 225

The likelihood of the observation k model (likelihood model) 226
 $p(\mathbf{y}_t^{m,k}|\mathbf{x}_t^{m,k})$ must be large for candidate regions with a his- 227
togram close to the reference histogram. Therefore, we intro- 228
duce the JS divergence [14] to measure the similarity between 229
the normalized candidate and reference histograms, $h_c^{\mathbf{x}_t}$ and 230
 $h_{c,\text{ref}}^k$, $c \in \{H, S, V\}$, respectively. Since, the JS divergence 231
is defined for probability distributions the histograms are nor- 232
malized, i.e., $\sum_N h_c^{\mathbf{x}_t} = 1$, where N denotes the number of 233
histogram bins. In contrast to the Kullback–Leibler divergence 234
[15], the JS divergence is symmetric and bounded between 0 235
and 1. The JS divergence between the normalized histograms is 236
defined as 237

$$\text{JS}_\pi(h_c^{\mathbf{x}_t}, h_{c,\text{ref}}^k) = H(\pi_1 h_c^{\mathbf{x}_t} + \pi_2 h_{c,\text{ref}}^k) - \pi_1 H(h_c^{\mathbf{x}_t}) - \pi_2 H(h_{c,\text{ref}}^k) \quad (7)$$

where $\pi_1 + \pi_2 = 1, \pi_i \geq 0$ and the function $H(\cdot)$ is the entropy 238
[15]. The JS divergence is computed for the histograms of the 239
H, S, and V space, and the observation likelihood is 240

$$p(\mathbf{y}_t^{m,k}|\mathbf{x}_t^{m,k}) \propto \exp -\lambda \left[\sum_{c \in \{H, S, V\}} \text{JS}_\pi(h_c^{\mathbf{x}_t^{m,k}}, h_{c,\text{ref}}^k) \right] \quad (8)$$

where parameter λ is chosen to be five and the weight π_i is 241
uniformly distributed. The number of bins of the histograms is 242
set to $N = 50$. The JS divergence provides a lower and upper 243
bound to the Bayes error and π_1 and π_2 can be viewed as 244
a priori probabilities in a classification problem [14]. 245

In contrast to the often used Bhattacharyya similarity coef- 246
ficient $\sqrt{1 - \sum_N \sqrt{h_c^{\mathbf{x}_t^{m,k}} h_{c,\text{ref}}^k}}$ [16], the JS divergence is not 247
so sensitive to local perturbations in the histogram (noise). This 248
is shown in Fig. 1 where we compute the JS divergence and 249
Bhattacharyya similarity coefficient on synthetic data. There- 250
fore, we sample two Gaussian distributions with $\mu_1 = -\mu_2$, 251

252 where μ_1 varies from 0 to 1.5, and unit variance. Noise is added
 253 to those distributions at a level of 10, 20, and 30 dB. Plots are
 254 averaged over 100 independent simulations.

255 D. Automatic Initialization of Objects

256 If an object enters the frame, a set of M particles and a refer-
 257 ence histogram for this object have to be initialized. Basically,
 258 the initialization of objects is automatically performed using the
 259 following simple low-level features.

260 1) Motion: The images are transformed to gray scale I_{x_t, y_t}^G .
 261 The motion feature is determined for each pixel located
 262 at x, y by the standard deviation over a time window
 263 T_w as $\sigma_{x, y}^t = \sigma(I_{x_t - T_w : t, y_t - T_w : t}^G)$. Applying an adaptive
 264 threshold $T_{\text{motion}} = 1/10 \max_{x, y \in IG} \sigma_{x, y}^t$ pixels with
 265 a value larger T_{motion} belong to regions where movement
 266 happens. However, $\max_{x, y \in IG} \sigma_{x, y}^t$ has to be sufficiently
 267 large so that motion exists at all. A binary motion image
 268 $I_{x_t, y_t}^{B_{\text{motion}}}$ after morphological closing is shown in Fig. 2.

269 2) Skin Color: The skin color of the people is modeled
 270 by a Gaussian mixture model [23] in the HSV
 271 color space. A Gaussian mixture model $p(\mathbf{z}|\Theta)$ is the
 272 weighted sum of $L > 1$ Gaussian components, $p(\mathbf{z}|\Theta) =$
 273 $\sum_{l=1}^L \alpha_l \mathcal{N}(\mathbf{z}|\mu_l, \Sigma_l)$, where $\mathbf{z} = [z_H, z_S, z_V]^T$ is the 3-D
 274 color vector of one image pixel, α_l corresponds to the
 275 weight of each component $l = 1, \dots, L$. These weights
 276 are constrained to be positive $\alpha_l \geq 0$ and $\sum_{l=1}^L \alpha_l = 1$.
 277 The Gaussian mixture is specified by the set of parameters
 278 $\Theta = \{\alpha_l, \mu_l, \Sigma_l\}_{l=1}^L$. These parameters are determined
 279 by the EM algorithm [24] from a face database.

280 Image pixels $\mathbf{z} \in I_{x_t, y_t}^{\text{HSV}}$ are classified according to their
 281 likelihood $p(\mathbf{z}|\Theta)$ using a threshold T_{skin} . The binary
 282 map $I_{x_t, y_t}^{B_{\text{skin}}}$ filtered with a morphological closing operator
 283 is presented in Fig. 2.

284 3) Object Size: We initialize a new object only for skin-
 285 colored moving regions with a size larger than T_{Area} .
 286 Additionally, we do not allow initialization of a new set of
 287 particles in regions where currently an object is tracked.
 288 To this end, a binary map $I_{x_t, y_t}^{B_{\text{prohibited}}}$ represents the areas
 289 where initialization is prohibited. The binary combination
 290 of all images $I_{x_t, y_t}^B = I_{x_t, y_t}^{B_{\text{motion}}} \cap I_{x_t, y_t}^{B_{\text{skin}}} \cap I_{x_t, y_t}^{B_{\text{prohibited}}}$ is
 291 used for extracting regions with an area larger T_{Area} . Tar-
 292 get objects are initialized for those regions, i.e., the ellipse
 293 size $(A_{\text{ref}}^k, B_{\text{ref}}^k)$ and the histograms $h_{c, \text{ref}}^k, c \in \{H, S, V\}$
 294 are determined from the region of the bounding ellipse.

295 Fig. 2 shows an example for the initialization of a new object.
 296 The original image $I_{x_t, y_t}^{\text{HSV}}$ is presented in (a). A person entering
 297 from the right side should be initialized. A second person in
 298 the middle of the image is already tracked. The binary images
 299 of the thresholded motion $I_{x_t, y_t}^{B_{\text{motion}}}$ and the skin-colored areas
 300 $I_{x_t, y_t}^{B_{\text{skin}}}$ are shown in (b) and (c), respectively. The reflections at
 301 the table and the movement of the curtain produce noise in the
 302 motion image. The color of the table and chairs intersects with
 303 the skin-color model. To guarantee successful initialization the
 304 lower part of the image—the region of the chairs and desk—has
 305 to be excluded. This is reasonable since nobody can enter in
 306 this area. Also, tracking is performed in the area above the

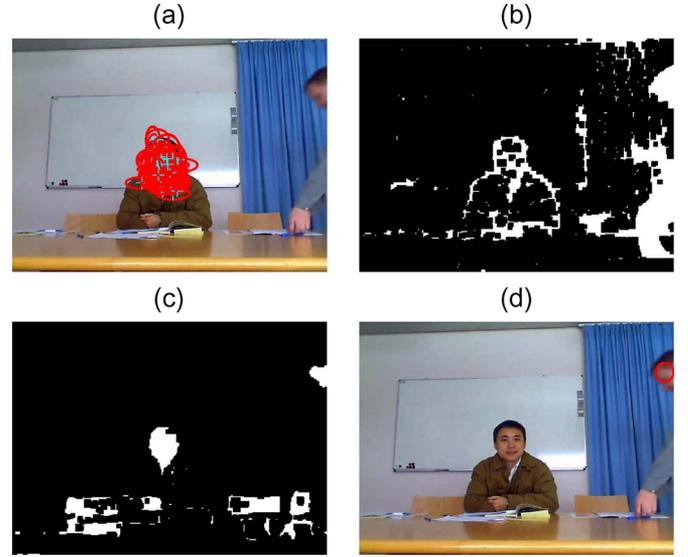


Fig. 2. Initialization of a new object. (a) Original image with one object already tracked. (b) Binary image of the thresholded motion $I_{x_t, y_t}^{B_{\text{motion}}}$. (c) Binary image of the skin-colored areas $I_{x_t, y_t}^{B_{\text{skin}}}$. (d) Image with region of initialized object.

chairs only. Finally, the region of the new initialized object is
 307 presented as ellipse in (d). Resizing of the images is performed
 308 for computing the features to speed up the initialization of
 309 objects. 310

311 1) Shortcomings: The objects are initialized when they en-
 312 ter the image. The reference histogram is taken during this
 313 initialization. There are the following shortcomings during
 314 initialization. 314

- 315 1) The camera is focused on the people sitting at the table
 316 and not on people walking behind the chairs. This means
 317 that walking persons appear blurred. 317
- 318 2) Entering persons are moving relatively fast. This also
 319 results in a degraded image quality (blurring). 319
- 320 3) During initialization, we normally get the side view of
 321 the person's head. When the person sits at the table the
 322 reference histogram is not necessarily a good model for
 323 the frontal view. 323

324 To deal with these shortcomings, we propose online learning
 325 to incrementally update the reference models of the tracked
 326 objects over time (see Section II-F). We perform this only in
 327 cases where no mutual occlusions between the tracked objects
 328 are existent. 328

329 E. Automatic Termination of Objects

330 Termination of particles is performed if the observation
 331 likelihood $p(\mathbf{y}_t^{m, k} | \mathbf{x}_t^{m, k})$ at state $\mathbf{x}_t^{m, k}$ drops below a predefined
 332 threshold T_{Kill} (e.g., 0.001), i.e., 332

$$p(\mathbf{y}_t^{m, k} | \mathbf{x}_t^{m, k}) = \begin{cases} 0, & \text{if } p(\mathbf{y}_t^{m, k} | \mathbf{x}_t^{m, k}) < T_{\text{Kill}} \\ p(\mathbf{y}_t^{m, k} | \mathbf{x}_t^{m, k}), & \text{otherwise.} \end{cases} \quad (9)$$

333 Particles with zero probability do not survive during resam-
 334 pling. If the tracked object leaves the field of view all M 334

335 particles of an object k are removed, i.e., $p(\mathbf{y}_t^{m,k} | \mathbf{x}_t^{m,k}) = 0$
 336 for all particles of object k .

337 F. Incremental Learning of Object Models

338 To handle the appearance change of the tracked objects over
 339 time, we use online learning to adapt the reference histograms
 340 $h_{c,\text{ref}}^k$, $c \in \{H, S, V\}$ (similar to [6]) and ellipse size A_{ref}^k and
 341 B_{ref}^k . Therefore, a learning rate α is introduced, and the model
 342 parameters for target object k are updated according to

$$h_{c,\text{ref}}^k = \alpha \hat{h}_c^k + (1 - \alpha) h_{c,\text{ref}}^k, \quad c \in \{H, S, V\} \quad (10)$$

$$A_{\text{ref}}^k = \alpha \hat{A}^k + (1 - \alpha) A_{\text{ref}}^k \quad (11)$$

$$B_{\text{ref}}^k = \alpha \hat{B}^k + (1 - \alpha) B_{\text{ref}}^k \quad (12)$$

343 where \hat{h}_c^k denotes the histogram and \hat{A}^k and \hat{B}^k are the prin-
 344 cipal axes of the bounding ellipse of the nonoccluded (i.e., no
 345 mutual occlusion between tracked objects) skin-colored region
 346 of the corresponding tracked object k located at $\{\mathbf{x}_t^{m,k}\}_{m=1}^M$.
 347 Again, this region has to be larger than T_{Area} . No update of
 348 the reference models is performed in the case where occlusion
 349 between the tracked objects occurs or the skin-colored region
 350 is not large enough. The latter condition is a simple way to
 351 ensure that the model update is only conducted for faces.
 352 This simplistic assumption can be appropriately extended by
 353 integrating more advanced face models.

354 The learning rate α introduces an *exponential forgetting*
 355 *process*, i.e., the contribution of a specific object exponentially
 356 decreases as it recedes into the past. Currently, the learning rate
 357 (value between 0 and 1) is fixed (a good value has been selected
 358 during experiments). However, α could be adapted depending
 359 on the dynamics of the scene.

360 **Algorithm 1** Particle Filter Tracking

361 **Input:** $I_{x_0:T, y_0:T}^{\text{HSV}}$ (Color image sequence $0 : T$),

362 Skin-color model Θ

363 **Parameters:** $M, N, \lambda, C, D, T_w, T_{\text{motion}}, T_{\text{skin}}, T_{\text{Area}},$

364 T_{Kill}, α

365 **Output:** $\{\{\mathbf{x}_{0:T}^{m,k}\}_{m=1}^M\}_{\forall k}$

366 $t \leftarrow 0$

367 $k \leftarrow 0$

368 **while** InitObjects **do**

369 $k \leftarrow k + 1$

370 Obtain: $h_{c,\text{ref}}^k : c \in \{H, S, V\}, A_{\text{ref}}^k, B_{\text{ref}}^k, \mathbf{x}_{\text{ref}}^k$

371 $\mathbf{x}_{t+1}^{m,k} \leftarrow \mathbf{x}_{\text{ref}}^k + C\mathbf{v}_t \quad \forall m = 1, \dots, M$ (Generate particles)

372 **end while**

373 $K \leftarrow k$

374 **for** $t = 1$ **to** T **do**

375 $w_t^{m,k} \propto p(\mathbf{y}_t^{m,k} | \mathbf{x}_t^{m,k})$

376 $\forall k = 1, \dots, K \quad \forall m = 1, \dots, M$

377 **while** KillObjects **do**

378 $k \leftarrow$ Determine object to terminate

379 Remove M particles $x_t^{m,k}$ of object k

380 Remove reference histogram and ellipse size:

381 $h_{c,\text{ref}}^k : c \in \{H, S, V\}, A_{\text{ref}}^k, B_{\text{ref}}^k$

382 $K \leftarrow K - 1$

383 **end while**



Fig. 3. Tracking scene. We track and initialize objects in the red rectangle.

for $k = 1$ **to** K **do** 384

$w_t^{m,k} \leftarrow w_t^{m,k} / \sum_{m'=1}^M w_t^{m',k} \quad \forall m = 1, \dots, M$ 385

$\{\mathbf{x}_t^{m,k}\}_{m=1}^M \leftarrow$ Resampling 386

(with replacement): $\{\mathbf{x}_t^{m,k}, w_t^{m,k}\}_{m=1}^M$ 387

$\mathbf{x}_{t+1}^{m,k} \leftarrow \mathbf{x}_t^{m,k} + C\mathbf{v}_t + (D/2M) \sum_{m'=1}^M (\mathbf{x}_t^{m',k} - \mathbf{x}_{t-1}^{m',k})$ 388

$\forall m = 1, \dots, M$ (Apply state-space dynamics) 389

if OnlineUpdate **then** 390

Determine: $\hat{h}_c^k : c \in \{H, S, V\}, \hat{A}^k, \hat{B}^k$ 391

$h_{c,\text{ref}}^k \leftarrow \alpha \hat{h}_c^k + (1 - \alpha) h_{c,\text{ref}}^k \quad c \in \{H, S, V\}$ 392

$A_{\text{ref}}^k \leftarrow \alpha \hat{A}^k + (1 - \alpha) A_{\text{ref}}^k$ 393

$B_{\text{ref}}^k \leftarrow \alpha \hat{B}^k + (1 - \alpha) B_{\text{ref}}^k$ 394

end if 395

end for 396

while InitObjects **do** 397

$K \leftarrow K + 1$ 398

Obtain: $h_{c,\text{ref}}^K : c \in \{H, S, V\}, A_{\text{ref}}^K, B_{\text{ref}}^K, \mathbf{x}_{\text{ref}}^K$ 399

$\mathbf{x}_{t+1}^{m,K} \leftarrow \mathbf{x}_{\text{ref}}^K + C\mathbf{v}_t \quad \forall m = 1, \dots, M$ (Generate 400

particles) 401

end while 402

end for 403

G. Implemented Tracker 404

In the following, we sketch our tracking approach for multi- 405
 ple objects (see Algorithm 1). The binary variable *InitObject* 406
 denotes that a new object for tracking has been detected. 407
KillObject is set if an object should be terminated. *OnlineUp-* 408
date indicates that object k located at $\{\mathbf{x}_t^{m,k}\}_{m=1}^M$ is nonoc- 409
 cluded, and the area of the skin-colored region is larger than 410
 T_{Area} , i.e., we perform online learning for reference model k . 411

Our implementation is related to the *dual estimation* problem 412
 [13], where both the states of multiple objects $\mathbf{x}_t^{m,k}$ and the 413
 parameters of the reference models are simultaneously esti- 414
 mated given the observations. At every time step, the particle 415
 filter estimates the states using the observation likelihood of 416
 the current reference models, while the online learning of the 417
 reference models is based on the current state estimates. 418

III. RELATIONSHIP TO GAS 419

GAs are optimization algorithms founded upon the principles 420
 of natural evolution discovered by Darwin. In nature, individ- 421
 uals have to adapt to their environment in order to survive in 422



Fig. 4. Tracking of people. Frames: 1, 416, 430, 449, 463, 491, 583, 609, 622, 637, 774, 844, 967, 975, 1182, 1400 (the frame number is assigned from left to right and top to bottom).

423 a process of further development. An introduction of GAs can
 424 be found in [25] and [26]. GA are stochastic procedures which
 425 have been successfully applied in many optimization tasks.
 426 GA operate on a population of potential solutions applying the
 427 principle of *survival of the fittest individual* to produce better
 428 and better approximations to the solution. At each generation, a
 429 new set of approximations is created by the process of selecting
 430 individuals according to their level of fitness in the problem
 431 domain and assembling them together using operators inspired
 432 from nature. This leads to the evolution of individuals that are
 433 better suited to their environment than the parent individuals
 434 they were created from. GA model the natural processes, such
 435 as selection, recombination, and mutation. Starting from an
 436 initial population $P(0)$, the sequence $P(0), P(1), \dots, P(t)$,
 437 $P(t + 1)$ is called population sequence or evolution. The end of
 438 an artificial evolution process is reached once the termination
 439 condition is met, and the result of the optimization task is
 440 available.

441 In this section, we want to point to the close relationship
 442 between GA and our particle filter for tracking. This analogy
 443 has been mentioned in [27]. As suggested in Section II, we
 444 treat the tracking of multiple objects completely independent,
 445 i.e., we have a set of M particles for each object k . In the GA
 446 framework, we can relate this to k instantiations of GA, one
 447 for each tracked object. Hence, each particle \mathbf{x}_t^m of object k
 448 represents one individual in the population $P(t)$ which is value
 449 encoded. The population size is M . A new genetic evolution

process is started once a new object is initialized for tracking 450
 (InitObject). The evolution process of the GA is terminated 451
 either at the end of the video ($t = T$) or when the set of 452
 individuals is not supported by the fitness value (KillObject). 453
 The observation likelihood $p(\mathbf{y}_t^{m,k} | \mathbf{x}_t^{m,k})$ denotes the fitness 454
 function to evaluate the individuals. However, the scope of GA 455
 for tracking is slightly different. GA are generally used to find a 456
 set of parameters for a given optimization task, i.e., the aim is to 457
 find the individual with the best fitness after the termination of 458
 the GA. Whereas, in the tracking case, the focus lies on the evo- 459
 lution of the individuals, i.e., the trajectory of the tracked object. 460

The selection operator directs the search toward promising 461
 regions in the search space. *Roulette Wheel Selection* [28] is a 462
 widely used selection method which is very similar to sampling 463
 with replacement as used in Section II. To each individual, a re- 464
 production probability according to $w_t^m \leftarrow w_t^m / \sum_{m'=1}^M w_t^{m'}$ 465
 is assigned. A roulette wheel is constructed with a slot size cor- 466
 responding to the individuals reproduction probability. Then, 467
 M uniformly distributed random numbers on the interval $[0, 1]$ 468
 are drawn and distributed according to their value around the 469
 wheel. The slots where they are placed to compose the subse- 470
 quent population $P(t)$. The state-space dynamics of the particle 471
 filter (see Section II-B) is modeled by the recombination and 472
 mutation operator. 473

The framework of the GA for tracking one object k is 474
 presented in Algorithm 1. The incremental learning of the 475
 reference model is omitted for the sake of brevity. 476



Fig. 5. Partial occlusions. Frames: 468, 616, 974, 4363 (the frame number is assigned from left to right and top to bottom).

477 **Algorithm 2** GA Tracking
 478 **Input:** $I_{x_{t:T}, y_{t:T}}^{\text{HSV}}$ (Color image sequence $t : T$),
 479 **Parameters:** $M, N, \lambda, C, D, T_{\text{Kill}}$
 480 **Output:** $\{\mathbf{x}_{t:T}^m\}_{m=1}^M$ (set of particle sequences $t : T$)
 481 Initialize population $P(t)$:
 482 $\mathbf{x}_t^m \leftarrow \mathbf{x}_{ref} + C\mathbf{v}_t \quad \forall m = 1, \dots, M$
 483 **while** $\text{KillObject} \cap t < T$ (Loop over image sequence) **do**
 484 Evaluate individuals:
 485 $w_t^m \leftarrow p(\mathbf{y}_t^m | \mathbf{x}_t^m) \quad \forall m = 1, \dots, M$
 486 Selection $P(t)$:
 487 $\{\mathbf{x}_t^m\}_{m=1}^M \leftarrow$ (Sampling with replacement) $\{\mathbf{x}_t^m, w_t^m\}_{m=1}^M$
 488 Recombination $P(t+1)$:
 489 $\mathbf{x}_{t+1}^m \leftarrow \mathbf{x}_t^m + (D/2M) \sum_{m'=1}^M (\mathbf{x}_t^{m'} - \mathbf{x}_t^{m-1})$
 490 $\forall m = 1, \dots, M$
 491 Mutation $P(t+1)$: $\mathbf{x}_{t+1}^m \leftarrow \mathbf{x}_{t+1}^m + C\mathbf{v}_t \quad \forall m = 1, \dots, M$
 492 $t \leftarrow t + 1$
 493 **end while**

494 IV. EXPERIMENTS

495 We present tracking results on meeting data in Section IV-A
 496 where we do both tracking of multiple persons and on-
 497 line adaptation of the reference models during tracking. In
 498 Section IV-B, we empirically show that the adaptation of the
 499 reference model during tracking (single object) of an indoor
 500 and outdoor scene results in a more robust tracking. Finally, in
 501 Section IV-C, tracking results using reference model adaptation
 502 for multiple objects of an outdoor scene are presented. For the
 503 outdoor scenes, we report the average standard deviation of
 504 the trajectories of independent tracking runs depending on the
 505 learning rate α .

506 A. Meeting Scenario

507 The meeting room layout is shown in Fig. 3. The red rec-
 508 tangle [region of interest (ROI)] in the image marks the frame
 509 where tracking and initialization of objects are performed. Peo-
 510 ple may enter and leave on both sides of the image. Currently,
 511 our tracker initializes a new target even if it enters from the



(a)



(b)



(c)

Fig. 6. Outdoor tracking. Frames: 7, 11, 12, 13, 14, 20, 42, 63, 80, 107, 136, 146, 158, 165, 192 (the frame number is assigned from left to right and top to bottom). (a) Original image sequence. (b) Tracking without reference model adaptation ($\alpha = 0$). (c) Tracking with online reference model learning ($\alpha = 0.2$).

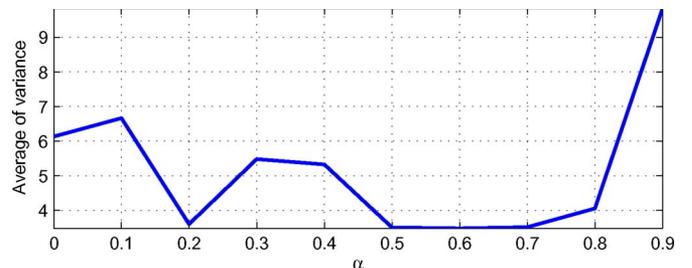


Fig. 7. Averaged standard deviation of the trajectories of 100 tracking runs depending on the reference model learning rate α .

bottom, e.g., a hand moving from the table into the ROI. The 512
 strong reflections at the table, chairs, and the white board cause 513
 noise in the motion image. 514

For testing the performance of our tracking approach, ten 515
 videos with ~ 7000 frames have been used. The resolution is 516
 640×480 pixels. The meeting room is equipped with a table 517
 and three chairs. We have different persons in each video. The 518
 people are coming from both sides into the frame moving 519

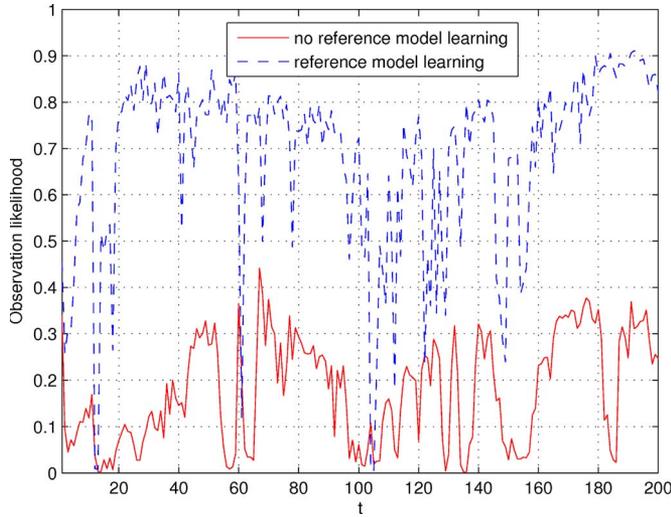


Fig. 8. Observation likelihood of outdoor sequence.

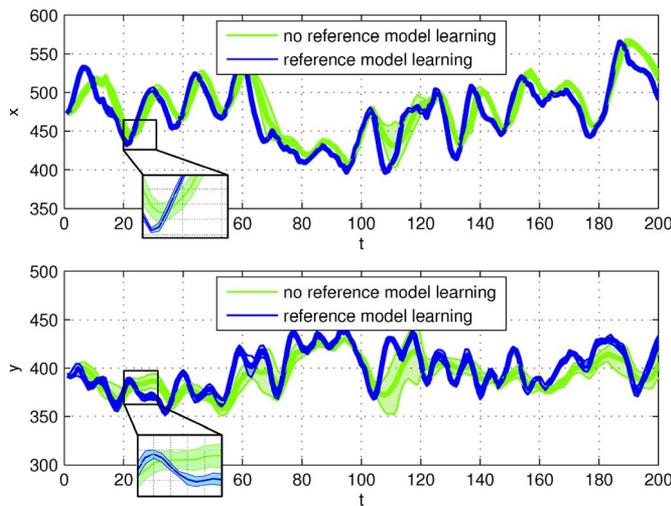


Fig. 9. Averaged trajectory with standard deviation in x and y of outdoor sequence (over ten runs).

520 to chairs and sit down. After a short discussion, people are
521 sequentially leaving the room, are coming back, sit down at
522 different chairs and so on. At the beginning, people may already
523 sit at the chairs. In this case, we have to automatically initialize
524 multiple objects at the very first frame.

525 Fig. 4 shows the result of the implemented tracker for one
526 video. All the initializations and terminations of objects are
527 performed automatically. The appearance of an object changes
528 over time. When entering the frame, we get the side view of
529 the person's head. After sitting down at the table, we have a
530 frontal view. We account for this by incrementally updating the
531 reference histogram during tracking. We perform this only in
532 the case where no mutual occlusions with other tracked objects
533 are existent. The participants were successfully tracked over
534 long image sequences.

535 First, the person on the left side stands up and leaves the room
536 on the right side (frame 416–491). When walking behind the
537 two sitting people, partial occlusions occur which do not cause
538 problems. Next, the person on the right (frame 583–637) leaves
539 the room on the left side. His face is again partially occluded



(a)



(b)



(c)

Fig. 10. Indoor tracking. Frames: 1, 12, 24, 31, 38, 41, 47, 54, 65, 71, 80, 107, 113, 120, 134 (the frame number is assigned from left to right and top to bottom). (a) Original image sequence. (b) Tracking without reference model adaptation ($\alpha = 0$). (c) Tracking with online reference model learning ($\alpha = 0.2$).

by the person in the middle. Then, the person on the center
540 chair leaves the room (frame 774). After that, a person on the
541 right side enters and sits at the left chair (frame 844). At frame
542 967, a small person is entering and moving to the chair in the
543 middle. Here, again, a partial occlusion occurs at frame 975, 544
544 which is also tackled. Finally, a person enters from the right
545 and sits down on the right chair (frame 1182, 1400). The partial
546 occlusions are shown in Fig. 5. Also, the blurred face of the
547 moving person in the back can be observed in this figure. The
548 reference model adaptation enables a more robust tracking. If
549 we do not update the models of the tracked objects over time,
550 the tracking fails in case of these partial occlusions. In [29],
551 occlusions are handled using multiple cameras for tracking
552 participants in a meeting. 553

B. Reference Model Adaptation for Single-Object Tracking 554

In the following, we show the benefit of the reference model
555 adaptation during tracking of a short indoor and outdoor se-
556 quence. In contrast to the meeting scenario, we restrict the
557

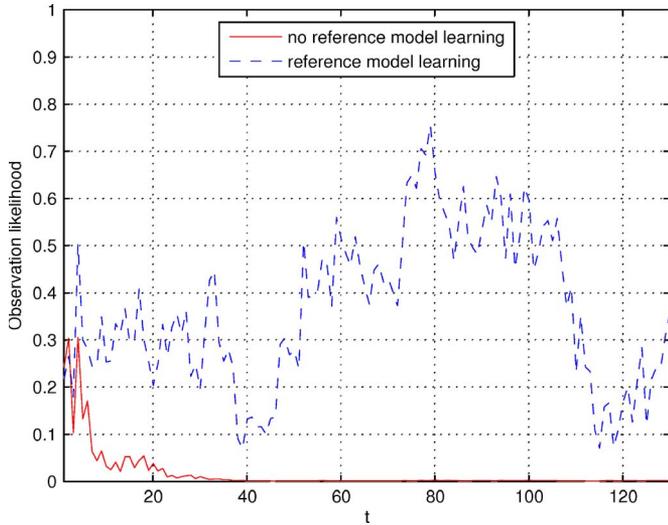


Fig. 11. Observation likelihood of indoor sequence.

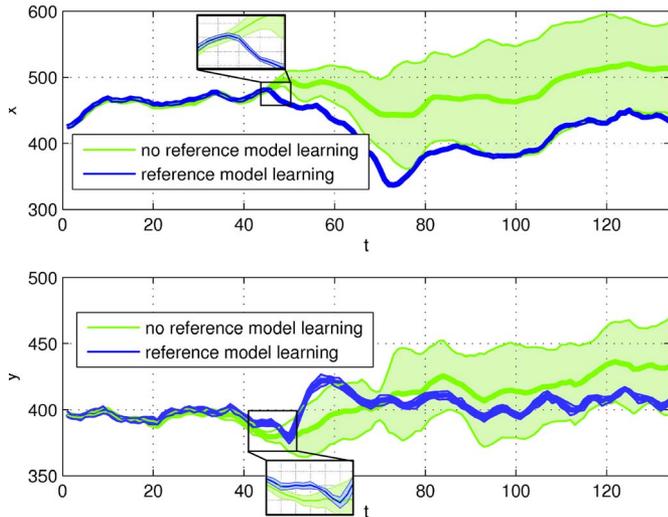


Fig. 12. Averaged trajectory with standard deviation in x and y of indoor sequence (over ten runs).

558 tracking to one single object, i.e., face. This means, in particular, that the automatic initialization and termination of the object is disabled. The object is initialized by hand in the first 561 frame.

562 Fig. 6(a) shows a short outdoor sequence where a person is moving behind a tree and two cars with strongly changing lighting conditions. We have a total occlusion of the face in frames 565 12 and 13 and a partial occluded face in frames 146 to 165. We repeated the tracking without and with reference model learning 567 ten times, and a typical result is shown in Fig. 6(b) and (c), 568 respectively. We use $M = 50$ particles for tracking, whereas only 15 particles with the best observation likelihood are shown 570 in the figures.

571 In Fig. 7, we present the average standard deviation of the trajectories over 100 tracking runs. The reference model learning rate α has been chosen in the range of $0, \dots, 0.6$ 574 (0 means that there is no learning). The optimal learning rate with respect to a low standard deviation of the trajectories over 576 100 independent runs is $\alpha = 0.2$ for this outdoor sequence.



(a)



(b)



(c)

Fig. 13. Outdoor tracking of multiple objects. Frames: 1, 12, 30, 47, 49, 51, 53, 57, 59, 79, 105, 107, 109, 111, 149 (the frame number is assigned from left to right and top to bottom). (a) Original image sequence. (b) Tracking without reference model adaptation ($\alpha = 0$). (c) Tracking with online reference model learning ($\alpha = 0.1$).

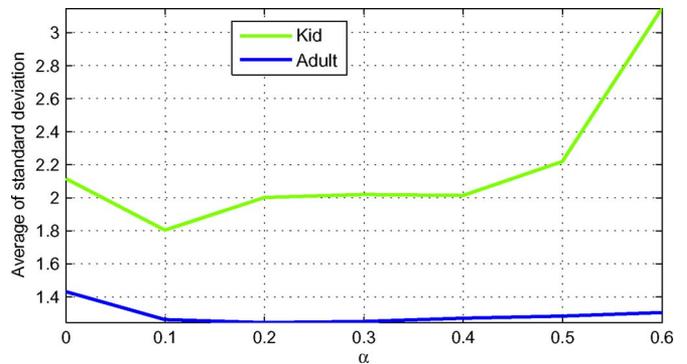


Fig. 14. Averaged standard deviation of the trajectories of ten tracking runs depending on the reference model learning rate α .

Fig. 8 shows the observation likelihood of the best particle 577 during tracking. At the complete occlusion (frames $t = 12$ and 578 $t = 13$) and the partial occlusion (frames $t = 145, \dots, 160$), the 579 observation likelihood drops, however, with reference model 580 learning a quick recovery is supported. 581

Fig. 9 summarizes the averaged trajectory with the standard deviation over ten different tracking runs performed for the outdoor scene. In the case of reference model learning, we observe in the video sequences that the tracking of the face gives highly similar trajectories. The standard deviation is small and approximately constant over time. However, if no learning of the reference model is performed, the standard deviation is large in certain time segments. This leads to the conclusion that model adaptation results in a more robust tracking.

Fig. 10(a) shows an indoor video where a person is moving on a corridor, and a tree causes partial occlusion of the tracked face. Additionally, the lighting conditions are strongly varying. The face is partially occluded by the tree in frames 37–50 and 110–126. Again, the tracking without and with reference model learning is repeated ten times, and a typical result is shown in Fig. 10(b) and (c), respectively. Only 15 particles with the best observation likelihood are visualized. The parameter setting is the same as in the previous experiments. The tracker without reference model refinement fails during the first occlusion in all ten runs, whereas the tracker with online model update is successful in all cases. The optimal learning rate α is set to 0.2 (established during experiments).

This can be also observed in the observation likelihood of the best particle over time (see Fig. 11) and in the averaged trajectory over ten tracking results (see Fig. 12).

C. Reference Model Adaptation for Multiple Object Tracking

We show tracking results for an outdoor scene where a kid is showing an adult dancing steps (see Fig. 13). A typical tracking result without and with reference model learning is shown in Fig. 13(b) and (c), respectively. Again, $M = 50$ particles are used, whereas only 15 particles with the best observation likelihood are shown in the figures. Similar as in the previous section, we did a repeatability test, i.e., we tracked the objects over ten independent runs. The tracked objects are initialized by hand in the very first frame.

Fig. 14 shows the average standard deviation of the trajectories of ten tracking runs using a learning rate α in the range of 0, . . . , 0.6. The optimal learning rate for the *Kid* and the *Adult* is $\alpha = 0.1$ and $\alpha = 0.2$, respectively. Currently, α is fixed for the whole image sequence. Ideally, α could be adapted depending on the dynamics of the scene.

623

V. CONCLUSION

We propose a robust visual tracking algorithm for multiple objects (faces of people) in a meeting scenario based on low-level features as skin color, target motion, and target size. Based on these features, automatic initialization and termination of objects is performed. For tracking a sampling importance resampling, particle filter has been used to propagate sample distributions over time. Furthermore, we use online learning of the target models to handle the appearance variability of the objects. We discuss the similarity between our implemented tracker and GAs. Each particle represents an individual in the GA framework. The evaluation function incorporates the observation likelihood model and the individual selection

process maps to the resampling procedure in the particle filter. The state-space dynamics is incorporated in the recombination and mutation operator of the GA. Numerous experiments on meeting data show the capabilities of the tracking approach. The participants were successfully tracked over long image sequences. Partial occlusions are handled by the algorithm. Additionally, we empirically show that the adaptation of the reference model during tracking of indoor and outdoor scenes results in a more robust tracking.

Future work concentrates on extending the tracker to other scenarios and to investigate an adaptive reference model learning rate α which depends on the dynamics of the scene. Furthermore, we aim to develop approaches for tackling occlusions.

ACKNOWLEDGMENT

This work was supported by the Austrian Science Fund (Project S106). The author would like to thank M. Grabner and M. Kepesi who collected the data during their involvement in the MISTRAL Project (www.mistral-project.at). The MISTRAL Project was funded by the Austrian Research Promotion Agency (www.ffg.at) within the strategic objective FIT-IT under Project 809264/9338. The author would also like to thank C. Kirchstätter for recording the indoor and outdoor video.

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Tracking of Multiple Targets Using Online Learning for Reference Model Adaptation

Franz Pernkopf

Abstract—Recently, much work has been done in multiple object tracking on the one hand and on reference model adaptation for a single-object tracker on the other side. In this paper, we do both tracking of multiple objects (faces of people) in a meeting scenario and online learning to incrementally update the models of the tracked objects to account for appearance changes during tracking. Additionally, we automatically initialize and terminate tracking of individual objects based on low-level features, i.e., face color, face size, and object movement. Many methods unlike our approach assume that the target region has been initialized by hand in the first frame. For tracking, a particle filter is incorporated to propagate sample distributions over time. We discuss the close relationship between our implemented tracker based on particle filters and genetic algorithms. Numerous experiments on meeting data demonstrate the capabilities of our tracking approach. Additionally, we provide an empirical verification of the reference model learning during tracking of indoor and outdoor scenes which supports a more robust tracking. Therefore, we report the average of the standard deviation of the trajectories over numerous tracking runs depending on the learning rate.

Index Terms—Genetic algorithms (GAs), multiple target tracking, particle filter, reference model learning, visual tracking.

I. INTRODUCTION

VISUAL tracking of multiple objects is concerned with maintaining the correct identity and location of a variable number of objects over time irrespective of occlusions and visual alterations. Lim *et al.* [1] differentiate between intrinsic and extrinsic appearance variability including pose variation, shape deformation of the object and illumination change, camera movement, occlusions, respectively.

In the past few years, particle filters have become the method of choice for tracking. Isard and Blake [2] introduced particle filtering (condensation algorithm). Many different sampling schemes have been suggested in the meantime. An overview about sampling schemes of particle filters and the relation to Kalman filters is provided in [3].

Recently, the main emphasis is on simultaneously tracking multiple objects and on online learning to adapt the reference models to the appearance changes, e.g., pose variation, illumination change. Lim *et al.* [1] introduce a single-object tracker, where the target representation—a low-dimensional eigenspace representation—is incrementally updated to model the appear-

ance variability. They assume, like most tracking algorithms, that the target region is initialized by hand in the first frame. Jepson *et al.* [4] use a Gaussian mixture model which is adapted using an online expectation maximization (EM) algorithm to account for appearance changes. Their WSL tracker uses a wavelet-based object model which is useful for tracking objects where regions of the objects (i.e., faces) are stable while other regions vary, e.g., mouth. McKenna *et al.* [5] employ Gaussian mixtures of the color distributions of the objects as adaptive model. In [6], simple color histograms are used to represent the objects (similar as in [7]). However, they introduce a simple update of the histograms to overcome the appearance changes of the object. All the aforementioned articles are focused on tracking a single object. For tracking multiple objects, most algorithms belong to one of the following three categories: 1) Multiple instances of a single-object tracker are used [8]. 2) All objects of interest are included in the state space [9]. A fixed number of objects is assumed. Varying number of objects result in a dynamic change of the dimension of the state space. 3) Most recently, the framework of particle filters is extended to capture multiple targets using a mixture model [10]. This mixture particle filter—where each component models an individual object—enables interaction between the components by the importance weights. In [11], this approach is extended by the Adaboost algorithm to learn the models of the targets. The information from Adaboost enables detection of objects entering the scene automatically. The mixture particle filter is further extended in [12] to handle mutual occlusions. They introduce a rectification technique to compensate for camera motions, a global nearest neighbor data association method to correctly identify object detections with existing tracks, and a mean-shift algorithm which accounts for more stable trajectories for reliable motion prediction.

In this paper, we do both tracking of multiple persons in a meeting scenario and online adaptation of the models to account for appearance changes during tracking. The tracking is based on low-level features such as skin color, object motion, and object size. Based on these features, automatic initialization and termination of objects are performed. The aim is to use as little prior knowledge as possible. For tracking, a particle filter is incorporated to propagate sample distributions over time. Our implementation is related to the *dual estimation* problem [13], where both the states of multiple objects and the parameters of the reference models are simultaneously estimated given the observations. At every time step, the particle filter estimates the states using the observation likelihood of the current reference models while the online learning of the reference models is based on the current state estimates. Additionally, we discuss

Manuscript received July 24, 2007; revised January 30, 2008. This work was supported by the Austrian Science Fund under Project P19737-N15.

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Digital Object Identifier 10.1109/TSMCB.2008.927281

94 the similarity between our implemented tracker based on parti-
 95 cle filters and genetic algorithms (GAs). We want to emphasize
 96 this close connection since approaches what have indepen-
 97 dently been developed in one community might turn out to be
 98 very useful for the other community and vice versa. Numerous
 99 experiments on meeting data demonstrate the capabilities of our
 100 tracking approach. Additionally, we empirically show that the
 101 adaptation of the reference model during tracking of an indoor
 102 and outdoor scenes results in a more robust tracking. For this,
 103 we report the average of the standard deviation of the trajecto-
 104 ries over numerous independent tracking runs depending on the
 105 learning rate.

106 The proposed approach differs from previous methods in
 107 several aspects. Recently, much work has been done in multiple
 108 object tracking on the one hand side and on reference model
 109 adaptation for a single-object tracker on the other side. In this
 110 paper, we do both tracking of multiple objects and online learn-
 111 ing to incrementally update the representation of the tracked ob-
 112 jects to model appearance changes. We use the Jensen–Shannon
 113 (JS) divergence [14] to measure the similarity between the
 114 tracked object and its reference model. Additionally, we discuss
 115 its advantages compared to the Kullback–Leibler divergence
 116 [15] and the Bhattacharyya similarity coefficient [16]. We auto-
 117 matically initialize and terminate tracking of individual objects
 118 based on low-level features, i.e., face color, face size, and object
 119 movement. Many methods unlike our approach assume that the
 120 target region has been initialized in the first frame.

121 This paper is organized as follows. Section II introduces
 122 the particle filter for multiple object tracking, the state-space
 123 dynamics, the observation model, automatic initialization and
 124 termination of objects, and the online learning of the mod-
 125 els for the tracked objects. Section II-G summarizes the im-
 126 plemented tracker on the basis of pseudocode. Section III
 127 sketches the relationship to GA. The tracking results on a
 128 meeting scenario and for indoor/outdoor scenes are presented in
 129 Section IV. Additionally, we provide empirical verification of
 130 the reference model learning in this section. Section V con-
 131 cludes this paper.

132 II. TRACKING USING PARTICLE FILTERS

133 In many applications the states of a dynamic system have
 134 to be estimated from a time series of noisy observations. The
 135 Kalman filter [13], [17] is a linear dynamical system [18] that
 136 provides a linear time-discrete filter that estimates the states
 137 online over time once observations become available. This
 138 filter is recursive in a sense that each current state estimate
 139 is computed from the previous estimate and the current ob-
 140 served data. In contrast to linear dynamical systems, the hidden
 141 Markov model [19] assumes a discrete state space. Recently,
 142 many extensions of the basic linear dynamical system have
 143 been proposed [13] to overcome the assumption of the linear-
 144 Gaussian model used for the observations and state transition,
 145 e.g., the extended Kalman filter, unscented Kalman filter, or
 146 the switching state-space model [20]. Another approach for
 147 filtering is to use sequential Monte Carlo methods which are
 148 also known as particle filters [21]. They are capable to deal with
 149 any nonlinearity or distribution.

A. Particle Filter

150

A particle filter is capable to deal with nonlinear non- 151
 Gaussian processes and has become popular for visual tracking. 152
 For tracking, the probability distribution that the object is in 153
 state \mathbf{x}_t at time t given the observations $\mathbf{y}_{0:t}$ up to time t is of 154
 interest. Hence, $p(\mathbf{x}_t|\mathbf{y}_{0:t})$ has to be constructed starting from 155
 the initial distribution $p(\mathbf{x}_0|\mathbf{y}_0) = p(\mathbf{x}_0)$. In Bayesian filtering, 156
 this can be formulated as iterative recursive process consisting 157
 of the prediction step 158

$$p(\mathbf{x}_t|\mathbf{y}_{0:t-1}) = \int p(\mathbf{x}_t|\mathbf{x}_{t-1})p(\mathbf{x}_{t-1}|\mathbf{y}_{0:t-1})d\mathbf{x}_{t-1} \quad (1)$$

and of the filtering step 159

$$p(\mathbf{x}_t|\mathbf{y}_{0:t}) = \frac{p(\mathbf{y}_t|\mathbf{x}_t)p(\mathbf{x}_t|\mathbf{y}_{0:t-1})}{\int p(\mathbf{y}_t|\mathbf{x}_t)p(\mathbf{x}_t|\mathbf{y}_{0:t-1})d\mathbf{x}_t} \quad (2)$$

where $p(\mathbf{x}_t|\mathbf{x}_{t-1})$ is the dynamic model describing the state- 160
 space evolution which corresponds to the evolution of the 161
 tracked object (see Section II-B) and $p(\mathbf{y}_t|\mathbf{x}_t)$ is the likelihood 162
 of an observation \mathbf{y}_t given the state \mathbf{x}_t (see observation model 163
 in Section II-C). 164

In particle filters $p(\mathbf{x}_t|\mathbf{y}_{0:t})$ of the filtering step is ap- 165
 proximated by a finite set of weighted samples, i.e., the 166
 particles, $\{\mathbf{x}_t^m, w_t^m\}_{m=1}^M$, where M is the number of sam- 167
 ples. Particles are sampled from a proposal distribution $\mathbf{x}_t^m \sim$ 168
 $q(\mathbf{x}_t|\mathbf{x}_{t-1}, \mathbf{y}_{0:t})$ (importance sampling) [3]. In each iteration, 169
 the importance weights are updated according to 170

$$w_t^m \propto \frac{p(\mathbf{y}_t|\mathbf{x}_t^m)p(\mathbf{x}_t^m|\mathbf{x}_{t-1}^m)}{q(\mathbf{x}_t^m|\mathbf{x}_{t-1}^m, \mathbf{y}_{0:t})}w_{t-1}^m \sum_{m=1}^M w_t^m = 1. \quad (3)$$

One simple choice for the proposal distribution is to take the 171
 prior density $q(\mathbf{x}_t^m|\mathbf{x}_{t-1}^m, \mathbf{y}_{0:t}) = p(\mathbf{x}_t^m|\mathbf{x}_{t-1}^m)$ (bootstrap filter). 172
 Hence, the weights are proportional to the likelihood model 173
 $p(\mathbf{y}_t|\mathbf{x}_t^m)$ 174

$$w_t^m \propto p(\mathbf{y}_t|\mathbf{x}_t^m)w_{t-1}^m. \quad (4)$$

The posterior filtered density $p(\mathbf{x}_t|\mathbf{y}_{1:t})$ can be approx- 175
 imated as 176

$$p(\mathbf{x}_t|\mathbf{y}_{1:t}) \approx \sum_{m=1}^M w_t^m \delta(\mathbf{x}_t - \mathbf{x}_t^m) \quad (5)$$

where $\delta(\mathbf{x}_t - \mathbf{x}_t^m)$ is the Dirac delta function with mass at \mathbf{x}_t^m . 177

We use resampling to reduce the *degeneracy problem* [3], 178
 [21]. We resample the particles $\{\mathbf{x}_t^m\}_{m=1}^M$ with replacement M 179
 times according to their weights w_t^m . The resulting particles 180
 $\{\mathbf{x}_t^m\}_{m=1}^M$ have uniformly distributed weights $w_t^m = 1/M$. 181
 Similar to the sampling importance resampling filter [3], we 182
 resample in every time step. This simplifies (4) to $w_t^m \propto$ 183
 $p(\mathbf{y}_t|\mathbf{x}_t^m)$ since $w_{t-1}^m = 1/M \quad \forall m$. 184

In the meeting scenario, we are interested in tracking the 185
 faces of multiple people. We treat the tracking of multiple 186
 objects completely independent, i.e., we assign a set of M 187
 particles to each tracked object k as $\{\{\mathbf{x}_t^{m,k}\}_{m=1}^M\}_{k=1}^K$, where 188
 K is the total number of tracked objects which dynamically 189

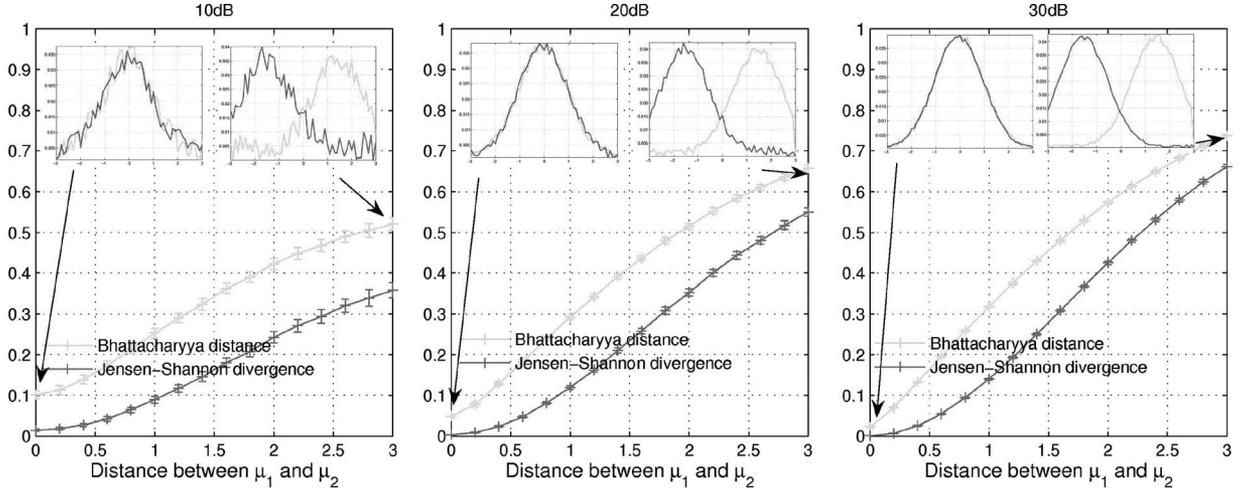


Fig. 1. JS divergence and Bhattacharyya similarity coefficient between two distributions estimated from samples. We added noise at a level of 10, 20, and 30 dB to the distributions.

190 changes over time. Hence, we use multiple instances of a single-
191 object tracker similar to [8].

192 B. State-Space Dynamics

193 The state sequence evolution $\{\mathbf{x}_t; t \in \mathbb{N}\}$ is assumed to be
194 a second-order autoregressive process which is used instead
195 of the first-order formalism ($p(\mathbf{x}_t|\mathbf{x}_{t-1})$) introduced in the
196 previous section. The second-order dynamics can be written as
197 first order by extending the state vector at time t with elements
198 from the state vector at time $t-1$.

199 We define the state vector at time t as $\mathbf{x}_t = [x_t \ y_t \ s_t^x \ s_t^y]^T$.
200 The location of the target at t is given as x_t, y_t , respectively,
201 and s_t^x, s_t^y denote the scale of the tracked region in the $x \times y$
202 image space. In our tracking approach, the transition model
203 corresponds to

$$\mathbf{x}_{t+1}^{m,k} = \mathbf{x}_t^{m,k} + C\mathbf{v}_t + \frac{D}{2M} \sum_{m'=1}^M (\mathbf{x}_t^{m',k} - \mathbf{x}_{t-1}^{m',k}) \quad (6)$$

204 where $\mathbf{v}_t \sim \mathcal{N}(0, \mathbf{I})$ is a simple Gaussian random noise model
205 and the term $1/2M \sum_{m'=1}^M (\mathbf{x}_t^{m',k} - \mathbf{x}_{t-1}^{m',k})$ captures the linear
206 evolution of object k from the particles of the previous time
207 step. Factor D models the influence of the linear evolution,
208 e.g., D is set to 0.5. The parameters of the random noise
209 model are set to $C = \text{diag}([10 \ 10 \ 0.03 \ 0.03])$ with the
210 units of [pixel/frame], [pixel/frame], [1/frame], and [1/frame],
211 respectively.

212 C. Observation Model

213 The shape of the tracked region is determined to be an ellipse
214 [4] since the tracking is focused on the faces of the individuals.
215 We assume that the principal axes of the ellipses are aligned
216 with the coordinate axes of the image. Similarly to [7], we use
217 the color histograms for modeling the target regions. Therefore,
218 we transform the image into the hue-saturation-value (HSV)
219 space [22]. For the sake of readability, we abuse the notation
220 and write the particle $\mathbf{x}_t^{m,k}$ as \mathbf{x}_t in this section. We build
221 an individual histogram for hue (H) $h_H^{\mathbf{x}_t}$, saturation (S) $h_S^{\mathbf{x}_t}$,

and value (V) $h_V^{\mathbf{x}_t}$ of the elliptic candidate region at \mathbf{x}_t . The 222
length of the principal axes of the ellipse are $A_{\text{ref}}^k s_t^x$ and $B_{\text{ref}}^k s_t^y$, 223
respectively, where A_{ref}^k and B_{ref}^k are the length of the ellipse 224
axes of the reference model of object k . 225

The likelihood of the observation k model (likelihood model) 226
 $p(\mathbf{y}_t^{m,k}|\mathbf{x}_t^{m,k})$ must be large for candidate regions with a his- 227
togram close to the reference histogram. Therefore, we intro- 228
duce the JS divergence [14] to measure the similarity between 229
the normalized candidate and reference histograms, $h_c^{\mathbf{x}_t}$ and 230
 $h_{c,\text{ref}}^k$, $c \in \{H, S, V\}$, respectively. Since, the JS divergence 231
is defined for probability distributions the histograms are nor- 232
malized, i.e., $\sum_N h_c^{\mathbf{x}_t} = 1$, where N denotes the number of 233
histogram bins. In contrast to the Kullback–Leibler divergence 234
[15], the JS divergence is symmetric and bounded between 0 235
and 1. The JS divergence between the normalized histograms is 236
defined as 237

$$\text{JS}_\pi(h_c^{\mathbf{x}_t}, h_{c,\text{ref}}^k) = H(\pi_1 h_c^{\mathbf{x}_t} + \pi_2 h_{c,\text{ref}}^k) - \pi_1 H(h_c^{\mathbf{x}_t}) - \pi_2 H(h_{c,\text{ref}}^k) \quad (7)$$

where $\pi_1 + \pi_2 = 1, \pi_i \geq 0$ and the function $H(\cdot)$ is the entropy 238
[15]. The JS divergence is computed for the histograms of the 239
H, S, and V space, and the observation likelihood is 240

$$p(\mathbf{y}_t^{m,k}|\mathbf{x}_t^{m,k}) \propto \exp -\lambda \left[\sum_{c \in \{H, S, V\}} \text{JS}_\pi(h_c^{\mathbf{x}_t}, h_{c,\text{ref}}^k) \right] \quad (8)$$

where parameter λ is chosen to be five and the weight π_i is 241
uniformly distributed. The number of bins of the histograms is 242
set to $N = 50$. The JS divergence provides a lower and upper 243
bound to the Bayes error and π_1 and π_2 can be viewed as 244
a priori probabilities in a classification problem [14]. 245

In contrast to the often used Bhattacharyya similarity coef- 246
ficient $\sqrt{1 - \sum_N \sqrt{h_c^{\mathbf{x}_t} h_{c,\text{ref}}^k}}$ [16], the JS divergence is not 247
so sensitive to local perturbations in the histogram (noise). This 248
is shown in Fig. 1 where we compute the JS divergence and 249
Bhattacharyya similarity coefficient on synthetic data. There- 250
fore, we sample two Gaussian distributions with $\mu_1 = -\mu_2$, 251

252 where μ_1 varies from 0 to 1.5, and unit variance. Noise is added
 253 to those distributions at a level of 10, 20, and 30 dB. Plots are
 254 averaged over 100 independent simulations.

255 D. Automatic Initialization of Objects

256 If an object enters the frame, a set of M particles and a refer-
 257 ence histogram for this object have to be initialized. Basically,
 258 the initialization of objects is automatically performed using the
 259 following simple low-level features.

260 1) Motion: The images are transformed to gray scale I_{x_t, y_t}^G .
 261 The motion feature is determined for each pixel located
 262 at x, y by the standard deviation over a time window
 263 T_w as $\sigma_{x, y}^t = \sigma(I_{x_t - T_w : t, y_t - T_w : t}^G)$. Applying an adaptive
 264 threshold $T_{\text{motion}} = 1/10 \max_{x, y \in IG} \sigma_{x, y}^t$ pixels with
 265 a value larger T_{motion} belong to regions where movement
 266 happens. However, $\max_{x, y \in IG} \sigma_{x, y}^t$ has to be sufficiently
 267 large so that motion exists at all. A binary motion image
 268 $I_{x_t, y_t}^{B_{\text{motion}}}$ after morphological closing is shown in Fig. 2.

269 2) Skin Color: The skin color of the people is modeled
 270 by a Gaussian mixture model [23] in the HSV
 271 color space. A Gaussian mixture model $p(\mathbf{z}|\Theta)$ is the
 272 weighted sum of $L > 1$ Gaussian components, $p(\mathbf{z}|\Theta) =$
 273 $\sum_{l=1}^L \alpha_l \mathcal{N}(\mathbf{z}|\mu_l, \Sigma_l)$, where $\mathbf{z} = [z_H, z_S, z_V]^T$ is the 3-D
 274 color vector of one image pixel, α_l corresponds to the
 275 weight of each component $l = 1, \dots, L$. These weights
 276 are constrained to be positive $\alpha_l \geq 0$ and $\sum_{l=1}^L \alpha_l = 1$.
 277 The Gaussian mixture is specified by the set of parameters
 278 $\Theta = \{\alpha_l, \mu_l, \Sigma_l\}_{l=1}^L$. These parameters are determined
 279 by the EM algorithm [24] from a face database.

280 Image pixels $\mathbf{z} \in I_{x_t, y_t}^{\text{HSV}}$ are classified according to their
 281 likelihood $p(\mathbf{z}|\Theta)$ using a threshold T_{skin} . The binary
 282 map $I_{x_t, y_t}^{B_{\text{skin}}}$ filtered with a morphological closing operator
 283 is presented in Fig. 2.

284 3) Object Size: We initialize a new object only for skin-
 285 colored moving regions with a size larger than T_{Area} .
 286 Additionally, we do not allow initialization of a new set of
 287 particles in regions where currently an object is tracked.
 288 To this end, a binary map $I_{x_t, y_t}^{B_{\text{prohibited}}}$ represents the areas
 289 where initialization is prohibited. The binary combination
 290 of all images $I_{x_t, y_t}^B = I_{x_t, y_t}^{B_{\text{motion}}} \cap I_{x_t, y_t}^{B_{\text{skin}}} \cap I_{x_t, y_t}^{B_{\text{prohibited}}}$ is
 291 used for extracting regions with an area larger T_{Area} . Tar-
 292 get objects are initialized for those regions, i.e., the ellipse
 293 size $(A_{\text{ref}}^k, B_{\text{ref}}^k)$ and the histograms $h_{c, \text{ref}}^k, c \in \{H, S, V\}$
 294 are determined from the region of the bounding ellipse.

295 Fig. 2 shows an example for the initialization of a new object.
 296 The original image $I_{x_t, y_t}^{\text{HSV}}$ is presented in (a). A person entering
 297 from the right side should be initialized. A second person in
 298 the middle of the image is already tracked. The binary images
 299 of the thresholded motion $I_{x_t, y_t}^{B_{\text{motion}}}$ and the skin-colored areas
 300 $I_{x_t, y_t}^{B_{\text{skin}}}$ are shown in (b) and (c), respectively. The reflections at
 301 the table and the movement of the curtain produce noise in the
 302 motion image. The color of the table and chairs intersects with
 303 the skin-color model. To guarantee successful initialization the
 304 lower part of the image—the region of the chairs and desk—has
 305 to be excluded. This is reasonable since nobody can enter in
 306 this area. Also, tracking is performed in the area above the

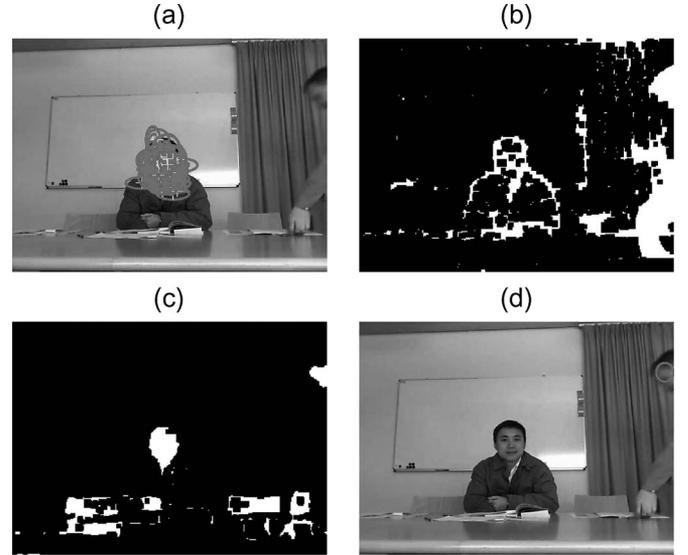


Fig. 2. Initialization of a new object. (a) Original image with one object already tracked. (b) Binary image of the thresholded motion $I_{x_t, y_t}^{B_{\text{motion}}}$. (c) Binary image of the skin-colored areas $I_{x_t, y_t}^{B_{\text{skin}}}$. (d) Image with region of initialized object.

chairs only. Finally, the region of the new initialized object is
 307 presented as ellipse in (d). Resizing of the images is performed
 308 for computing the features to speed up the initialization of
 309 objects. 310

311 1) Shortcomings: The objects are initialized when they en-
 312 ter the image. The reference histogram is taken during this
 313 initialization. There are the following shortcomings during
 314 initialization. 314

- 315 1) The camera is focused on the people sitting at the table
 316 and not on people walking behind the chairs. This means
 317 that walking persons appear blurred. 317
- 318 2) Entering persons are moving relatively fast. This also
 319 results in a degraded image quality (blurring). 319
- 320 3) During initialization, we normally get the side view of
 321 the person's head. When the person sits at the table the
 322 reference histogram is not necessarily a good model for
 323 the frontal view. 323

324 To deal with these shortcomings, we propose online learning
 325 to incrementally update the reference models of the tracked
 326 objects over time (see Section II-F). We perform this only in
 327 cases where no mutual occlusions between the tracked objects
 328 are existent. 328

329 E. Automatic Termination of Objects

330 Termination of particles is performed if the observation
 331 likelihood $p(\mathbf{y}_t^{m, k} | \mathbf{x}_t^{m, k})$ at state $\mathbf{x}_t^{m, k}$ drops below a predefined
 332 threshold T_{Kill} (e.g., 0.001), i.e., 332

$$p(\mathbf{y}_t^{m, k} | \mathbf{x}_t^{m, k}) = \begin{cases} 0, & \text{if } p(\mathbf{y}_t^{m, k} | \mathbf{x}_t^{m, k}) < T_{\text{Kill}} \\ p(\mathbf{y}_t^{m, k} | \mathbf{x}_t^{m, k}), & \text{otherwise.} \end{cases} \quad (9)$$

333 Particles with zero probability do not survive during resam-
 334 pling. If the tracked object leaves the field of view all M 334

335 particles of an object k are removed, i.e., $p(\mathbf{y}_t^{m,k} | \mathbf{x}_t^{m,k}) = 0$
 336 for all particles of object k .

337 F. Incremental Learning of Object Models

338 To handle the appearance change of the tracked objects over
 339 time, we use online learning to adapt the reference histograms
 340 $h_{c,\text{ref}}^k$, $c \in \{H, S, V\}$ (similar to [6]) and ellipse size A_{ref}^k and
 341 B_{ref}^k . Therefore, a learning rate α is introduced, and the model
 342 parameters for target object k are updated according to

$$h_{c,\text{ref}}^k = \alpha \hat{h}_c^k + (1 - \alpha) h_{c,\text{ref}}^k, \quad c \in \{H, S, V\} \quad (10)$$

$$A_{\text{ref}}^k = \alpha \hat{A}^k + (1 - \alpha) A_{\text{ref}}^k \quad (11)$$

$$B_{\text{ref}}^k = \alpha \hat{B}^k + (1 - \alpha) B_{\text{ref}}^k \quad (12)$$

343 where \hat{h}_c^k denotes the histogram and \hat{A}^k and \hat{B}^k are the prin-
 344 cipal axes of the bounding ellipse of the nonoccluded (i.e., no
 345 mutual occlusion between tracked objects) skin-colored region
 346 of the corresponding tracked object k located at $\{\mathbf{x}_t^{m,k}\}_{m=1}^M$.
 347 Again, this region has to be larger than T_{Area} . No update of
 348 the reference models is performed in the case where occlusion
 349 between the tracked objects occurs or the skin-colored region
 350 is not large enough. The latter condition is a simple way to
 351 ensure that the model update is only conducted for faces.
 352 This simplistic assumption can be appropriately extended by
 353 integrating more advanced face models.

354 The learning rate α introduces an *exponential forgetting*
 355 *process*, i.e., the contribution of a specific object exponentially
 356 decreases as it recedes into the past. Currently, the learning rate
 357 (value between 0 and 1) is fixed (a good value has been selected
 358 during experiments). However, α could be adapted depending
 359 on the dynamics of the scene.

360 **Algorithm 1** Particle Filter Tracking

361 **Input:** $I_{x_0:T, y_0:T}^{\text{HSV}}$ (Color image sequence $0 : T$),
 362 Skin-color model Θ
 363 **Parameters:** $M, N, \lambda, C, D, T_w, T_{\text{motion}}, T_{\text{skin}}, T_{\text{Area}},$
 364 T_{Kill}, α
 365 **Output:** $\{\{\mathbf{x}_{0:T}^{m,k}\}_{m=1}^M\}_{\forall k}$
 366 $t \leftarrow 0$
 367 $k \leftarrow 0$
 368 **while** InitObjects **do**
 369 $k \leftarrow k + 1$
 370 Obtain: $h_{c,\text{ref}}^k : c \in \{H, S, V\}, A_{\text{ref}}^k, B_{\text{ref}}^k, \mathbf{x}_{\text{ref}}^k$
 371 $\mathbf{x}_{t+1}^{m,k} \leftarrow \mathbf{x}_{\text{ref}}^k + C\mathbf{v}_t \quad \forall m = 1, \dots, M$ (Generate particles)
 372 **end while**
 373 $K \leftarrow k$
 374 **for** $t = 1$ **to** T **do**
 375 $w_t^{m,k} \propto p(\mathbf{y}_t^{m,k} | \mathbf{x}_t^{m,k})$
 376 $\forall k = 1, \dots, K \quad \forall m = 1, \dots, M$
 377 **while** KillObjects **do**
 378 $k \leftarrow$ Determine object to terminate
 379 Remove M particles $x_t^{m,k}$ of object k
 380 Remove reference histogram and ellipse size:
 381 $h_{c,\text{ref}}^k : c \in \{H, S, V\}, A_{\text{ref}}^k, B_{\text{ref}}^k$
 382 $K \leftarrow K - 1$
 383 **end while**

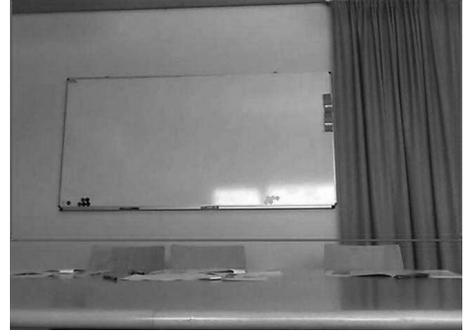


Fig. 3. Tracking scene. We track and initialize objects in the red rectangle.

for $k = 1$ **to** K **do** 384
 $w_t^{m,k} \leftarrow w_t^{m,k} / \sum_{m'=1}^M w_t^{m',k} \quad \forall m = 1, \dots, M$ 385
 $\{\mathbf{x}_t^{m,k}\}_{m=1}^M \leftarrow$ Resampling 386
 (with replacement): $\{\mathbf{x}_t^{m,k}, w_t^{m,k}\}_{m=1}^M$ 387
 $\mathbf{x}_{t+1}^{m,k} \leftarrow \mathbf{x}_t^{m,k} + C\mathbf{v}_t + (D/2M) \sum_{m'=1}^M (\mathbf{x}_t^{m',k} - \mathbf{x}_{t-1}^{m',k})$ 388
 $\forall m = 1, \dots, M$ (Apply state-space dynamics) 389
if OnlineUpdate **then** 390
 Determine: $\hat{h}_c^k : c \in \{H, S, V\}, \hat{A}^k, \hat{B}^k$ 391
 $h_{c,\text{ref}}^k \leftarrow \alpha \hat{h}_c^k + (1 - \alpha) h_{c,\text{ref}}^k \quad c \in \{H, S, V\}$ 392
 $A_{\text{ref}}^k \leftarrow \alpha \hat{A}^k + (1 - \alpha) A_{\text{ref}}^k$ 393
 $B_{\text{ref}}^k \leftarrow \alpha \hat{B}^k + (1 - \alpha) B_{\text{ref}}^k$ 394
end if 395
end for 396
while InitObjects **do** 397
 $K \leftarrow K + 1$ 398
 Obtain: $h_{c,\text{ref}}^K : c \in \{H, S, V\}, A_{\text{ref}}^K, B_{\text{ref}}^K, \mathbf{x}_{\text{ref}}^K$ 399
 $\mathbf{x}_{t+1}^{m,K} \leftarrow \mathbf{x}_{\text{ref}}^K + C\mathbf{v}_t \quad \forall m = 1, \dots, M$ (Generate 400
 particles) 401
end while 402
end for 403

G. Implemented Tracker 404

In the following, we sketch our tracking approach for multi- 405
 ple objects (see Algorithm 1). The binary variable *InitObject* 406
 denotes that a new object for tracking has been detected. 407
KillObject is set if an object should be terminated. *OnlineUp-* 408
date indicates that object k located at $\{\mathbf{x}_t^{m,k}\}_{m=1}^M$ is nonoc- 409
 cluded, and the area of the skin-colored region is larger than 410
 T_{Area} , i.e., we perform online learning for reference model k . 411

Our implementation is related to the *dual estimation* problem 412
 [13], where both the states of multiple objects $\mathbf{x}_t^{m,k}$ and the 413
 parameters of the reference models are simultaneously esti- 414
 mated given the observations. At every time step, the particle 415
 filter estimates the states using the observation likelihood of 416
 the current reference models, while the online learning of the 417
 reference models is based on the current state estimates. 418

III. RELATIONSHIP TO GAS 419

GAs are optimization algorithms founded upon the principles 420
 of natural evolution discovered by Darwin. In nature, individ- 421
 uals have to adapt to their environment in order to survive in 422



Fig. 4. Tracking of people. Frames: 1, 416, 430, 449, 463, 491, 583, 609, 622, 637, 774, 844, 967, 975, 1182, 1400 (the frame number is assigned from left to right and top to bottom).

423 a process of further development. An introduction of GAs can
 424 be found in [25] and [26]. GA are stochastic procedures which
 425 have been successfully applied in many optimization tasks.
 426 GA operate on a population of potential solutions applying the
 427 principle of *survival of the fittest individual* to produce better
 428 and better approximations to the solution. At each generation, a
 429 new set of approximations is created by the process of selecting
 430 individuals according to their level of fitness in the problem
 431 domain and assembling them together using operators inspired
 432 from nature. This leads to the evolution of individuals that are
 433 better suited to their environment than the parent individuals
 434 they were created from. GA model the natural processes, such
 435 as selection, recombination, and mutation. Starting from an
 436 initial population $P(0)$, the sequence $P(0), P(1), \dots, P(t)$,
 437 $P(t + 1)$ is called population sequence or evolution. The end of
 438 an artificial evolution process is reached once the termination
 439 condition is met, and the result of the optimization task is
 440 available.

441 In this section, we want to point to the close relationship
 442 between GA and our particle filter for tracking. This analogy
 443 has been mentioned in [27]. As suggested in Section II, we
 444 treat the tracking of multiple objects completely independent,
 445 i.e., we have a set of M particles for each object k . In the GA
 446 framework, we can relate this to k instantiations of GA, one
 447 for each tracked object. Hence, each particle \mathbf{x}_t^m of object k
 448 represents one individual in the population $P(t)$ which is value
 449 encoded. The population size is M . A new genetic evolution

process is started once a new object is initialized for tracking 450
 (InitObject). The evolution process of the GA is terminated 451
 either at the end of the video ($t = T$) or when the set of 452
 individuals is not supported by the fitness value (KillObject). 453
 The observation likelihood $p(\mathbf{y}_t^{m,k} | \mathbf{x}_t^{m,k})$ denotes the fitness 454
 function to evaluate the individuals. However, the scope of GA 455
 for tracking is slightly different. GA are generally used to find a 456
 set of parameters for a given optimization task, i.e., the aim is to 457
 find the individual with the best fitness after the termination of 458
 the GA. Whereas, in the tracking case, the focus lies on the evo- 459
 lution of the individuals, i.e., the trajectory of the tracked object. 460

The selection operator directs the search toward promising 461
 regions in the search space. *Roulette Wheel Selection* [28] is a 462
 widely used selection method which is very similar to sampling 463
 with replacement as used in Section II. To each individual, a re- 464
 production probability according to $w_t^m \leftarrow w_t^m / \sum_{m'=1}^M w_t^{m'}$ 465
 is assigned. A roulette wheel is constructed with a slot size cor- 466
 responding to the individuals reproduction probability. Then, 467
 M uniformly distributed random numbers on the interval $[0, 1]$ 468
 are drawn and distributed according to their value around the 469
 wheel. The slots where they are placed to compose the subse- 470
 quent population $P(t)$. The state-space dynamics of the particle 471
 filter (see Section II-B) is modeled by the recombination and 472
 mutation operator. 473

The framework of the GA for tracking one object k is 474
 presented in Algorithm 1. The incremental learning of the 475
 reference model is omitted for the sake of brevity. 476



Fig. 5. Partial occlusions. Frames: 468, 616, 974, 4363 (the frame number is assigned from left to right and top to bottom).

477 **Algorithm 2** GA Tracking
 478 **Input:** $I_{x_t:T, y_t:T}^{\text{HSV}}$ (Color image sequence $t : T$),
 479 **Parameters:** $M, N, \lambda, C, D, T_{\text{Kill}}$
 480 **Output:** $\{\mathbf{x}_{t:T}^m\}_{m=1}^M$ (set of particle sequences $t : T$)
 481 Initialize population $P(t)$:
 482 $\mathbf{x}_t^m \leftarrow \mathbf{x}_{\text{ref}} + C\mathbf{v}_t \quad \forall m = 1, \dots, M$
 483 **while** $\text{KillObject} \cap t < T$ (Loop over image sequence) **do**
 484 Evaluate individuals:
 485 $w_t^m \leftarrow p(\mathbf{y}_t^m | \mathbf{x}_t^m) \quad \forall m = 1, \dots, M$
 486 Selection $P(t)$:
 487 $\{\mathbf{x}_t^m\}_{m=1}^M \leftarrow$ (Sampling with replacement) $\{\mathbf{x}_t^m, w_t^m\}_{m=1}^M$
 488 Recombination $P(t+1)$:
 489 $\mathbf{x}_{t+1}^m \leftarrow \mathbf{x}_t^m + (D/2M) \sum_{m'=1}^M (\mathbf{x}_t^{m'} - \mathbf{x}_{t-1}^{m'})$
 490 $\forall m = 1, \dots, M$
 491 Mutation $P(t+1)$: $\mathbf{x}_{t+1}^m \leftarrow \mathbf{x}_{t+1}^m + C\mathbf{v}_t \quad \forall m = 1, \dots, M$
 492 $t \leftarrow t + 1$
 493 **end while**

494 IV. EXPERIMENTS

495 We present tracking results on meeting data in Section IV-A
 496 where we do both tracking of multiple persons and on-
 497 line adaptation of the reference models during tracking. In
 498 Section IV-B, we empirically show that the adaptation of the
 499 reference model during tracking (single object) of an indoor
 500 and outdoor scene results in a more robust tracking. Finally, in
 501 Section IV-C, tracking results using reference model adaptation
 502 for multiple objects of an outdoor scene are presented. For the
 503 outdoor scenes, we report the average standard deviation of
 504 the trajectories of independent tracking runs depending on the
 505 learning rate α .

506 A. Meeting Scenario

507 The meeting room layout is shown in Fig. 3. The red rec-
 508 tangle [region of interest (ROI)] in the image marks the frame
 509 where tracking and initialization of objects are performed. Peo-
 510 ple may enter and leave on both sides of the image. Currently,
 511 our tracker initializes a new target even if it enters from the



(a)



(b)



(c)

Fig. 6. Outdoor tracking. Frames: 7, 11, 12, 13, 14, 20, 42, 63, 80, 107, 136, 146, 158, 165, 192 (the frame number is assigned from left to right and top to bottom). (a) Original image sequence. (b) Tracking without reference model adaptation ($\alpha = 0$). (c) Tracking with online reference model learning ($\alpha = 0.2$).

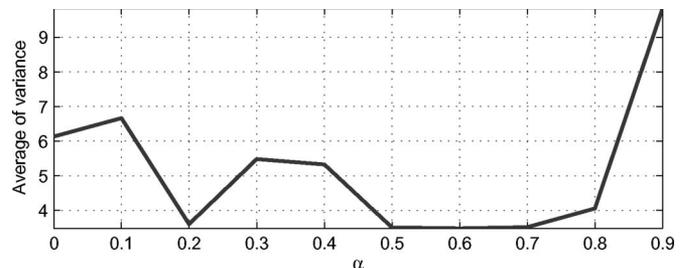


Fig. 7. Averaged standard deviation of the trajectories of 100 tracking runs depending on the reference model learning rate α .

bottom, e.g., a hand moving from the table into the ROI. The 512
 strong reflections at the table, chairs, and the white board cause 513
 noise in the motion image. 514

For testing the performance of our tracking approach, ten 515
 videos with ~ 7000 frames have been used. The resolution is 516
 640×480 pixels. The meeting room is equipped with a table 517
 and three chairs. We have different persons in each video. The 518
 people are coming from both sides into the frame moving 519

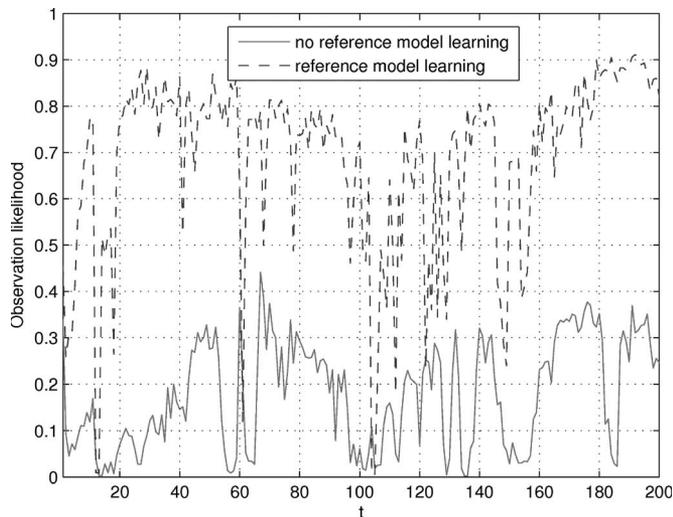


Fig. 8. Observation likelihood of outdoor sequence.

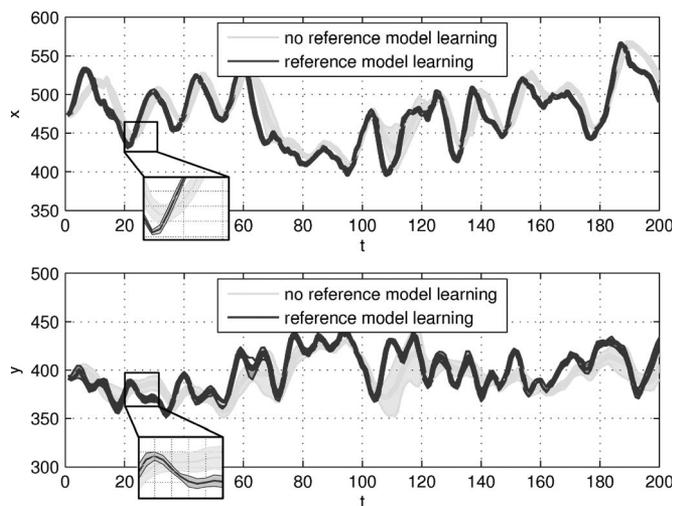


Fig. 9. Averaged trajectory with standard deviation in x and y of outdoor sequence (over ten runs).

520 to chairs and sit down. After a short discussion, people are
521 sequentially leaving the room, are coming back, sit down at
522 different chairs and so on. At the beginning, people may already
523 sit at the chairs. In this case, we have to automatically initialize
524 multiple objects at the very first frame.

525 Fig. 4 shows the result of the implemented tracker for one
526 video. All the initializations and terminations of objects are
527 performed automatically. The appearance of an object changes
528 over time. When entering the frame, we get the side view of
529 the person's head. After sitting down at the table, we have a
530 frontal view. We account for this by incrementally updating the
531 reference histogram during tracking. We perform this only in
532 the case where no mutual occlusions with other tracked objects
533 are existent. The participants were successfully tracked over
534 long image sequences.

535 First, the person on the left side stands up and leaves the room
536 on the right side (frame 416–491). When walking behind the
537 two sitting people, partial occlusions occur which do not cause
538 problems. Next, the person on the right (frame 583–637) leaves
539 the room on the left side. His face is again partially occluded



(a)



(b)



(c)

Fig. 10. Indoor tracking. Frames: 1, 12, 24, 31, 38, 41, 47, 54, 65, 71, 80, 107, 113, 120, 134 (the frame number is assigned from left to right and top to bottom). (a) Original image sequence. (b) Tracking without reference model adaptation ($\alpha = 0$). (c) Tracking with online reference model learning ($\alpha = 0.2$).

by the person in the middle. Then, the person on the center
540 chair leaves the room (frame 774). After that, a person on the
541 right side enters and sits at the left chair (frame 844). At frame
542 967, a small person is entering and moving to the chair in the
543 middle. Here, again, a partial occlusion occurs at frame 975, 544
544 which is also tackled. Finally, a person enters from the right
545 and sits down on the right chair (frame 1182, 1400). The partial
546 occlusions are shown in Fig. 5. Also, the blurred face of the
547 moving person in the back can be observed in this figure. The
548 reference model adaptation enables a more robust tracking. If
549 we do not update the models of the tracked objects over time,
550 the tracking fails in case of these partial occlusions. In [29],
551 occlusions are handled using multiple cameras for tracking
552 participants in a meeting. 553

B. Reference Model Adaptation for Single-Object Tracking 554

In the following, we show the benefit of the reference model
555 adaptation during tracking of a short indoor and outdoor se-
556 quence. In contrast to the meeting scenario, we restrict the
557

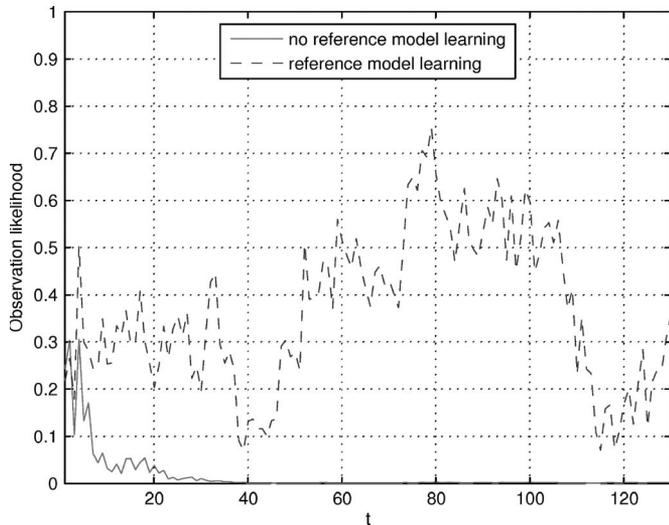


Fig. 11. Observation likelihood of indoor sequence.

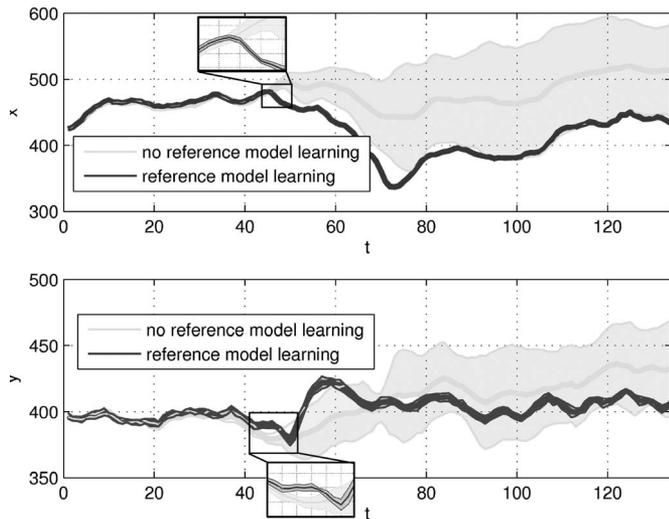
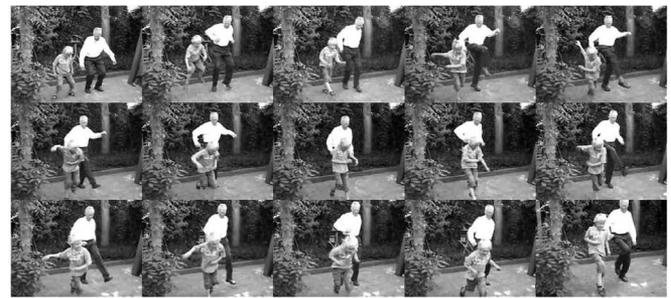


Fig. 12. Averaged trajectory with standard deviation in x and y of indoor sequence (over ten runs).

558 tracking to one single object, i.e., face. This means, in particular, that the automatic initialization and termination of the object is disabled. The object is initialized by hand in the first 561 frame.

562 Fig. 6(a) shows a short outdoor sequence where a person is moving behind a tree and two cars with strongly changing lighting conditions. We have a total occlusion of the face in frames 565 12 and 13 and a partial occluded face in frames 146 to 165. We 566 repeated the tracking without and with reference model learning 567 ten times, and a typical result is shown in Fig. 6(b) and (c), 568 respectively. We use $M = 50$ particles for tracking, whereas 569 only 15 particles with the best observation likelihood are shown 570 in the figures.

571 In Fig. 7, we present the average standard deviation of 572 the trajectories over 100 tracking runs. The reference model 573 learning rate α has been chosen in the range of $0, \dots, 0.6$ 574 (0 means that there is no learning). The optimal learning rate 575 with respect to a low standard deviation of the trajectories over 576 100 independent runs is $\alpha = 0.2$ for this outdoor sequence.



(a)



(b)



(c)

Fig. 13. Outdoor tracking of multiple objects. Frames: 1, 12, 30, 47, 49, 51, 53, 57, 59, 79, 105, 107, 109, 111, 149 (the frame number is assigned from left to right and top to bottom). (a) Original image sequence. (b) Tracking without reference model adaptation ($\alpha = 0$). (c) Tracking with online reference model learning ($\alpha = 0.1$).

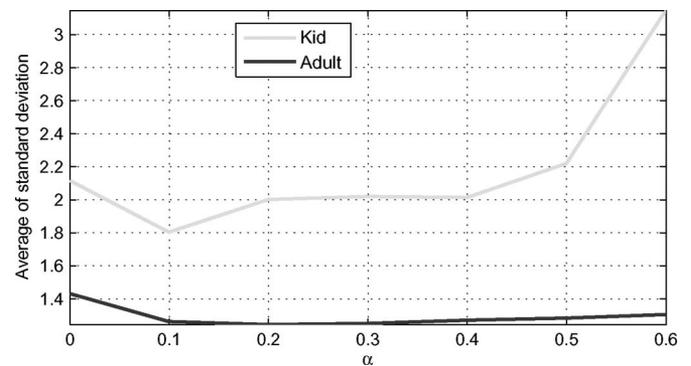


Fig. 14. Averaged standard deviation of the trajectories of ten tracking runs depending on the reference model learning rate α .

Fig. 8 shows the observation likelihood of the best particle 577 during tracking. At the complete occlusion (frames $t = 12$ and 578 $t = 13$) and the partial occlusion (frames $t = 145, \dots, 160$), the 579 observation likelihood drops, however, with reference model 580 learning a quick recovery is supported. 581

Fig. 9 summarizes the averaged trajectory with the standard deviation over ten different tracking runs performed for the outdoor scene. In the case of reference model learning, we observe in the video sequences that the tracking of the face gives highly similar trajectories. The standard deviation is small and approximately constant over time. However, if no learning of the reference model is performed, the standard deviation is large in certain time segments. This leads to the conclusion that model adaptation results in a more robust tracking.

Fig. 10(a) shows an indoor video where a person is moving on a corridor, and a tree causes partial occlusion of the tracked face. Additionally, the lighting conditions are strongly varying. The face is partially occluded by the tree in frames 37–50 and 110–126. Again, the tracking without and with reference model learning is repeated ten times, and a typical result is shown in Fig. 10(b) and (c), respectively. Only 15 particles with the best observation likelihood are visualized. The parameter setting is the same as in the previous experiments. The tracker without reference model refinement fails during the first occlusion in all ten runs, whereas the tracker with online model update is successful in all cases. The optimal learning rate α is set to 0.2 (established during experiments).

This can be also observed in the observation likelihood of the best particle over time (see Fig. 11) and in the averaged trajectory over ten tracking results (see Fig. 12).

C. Reference Model Adaptation for Multiple Object Tracking

We show tracking results for an outdoor scene where a kid is showing an adult dancing steps (see Fig. 13). A typical tracking result without and with reference model learning is shown in Fig. 13(b) and (c), respectively. Again, $M = 50$ particles are used, whereas only 15 particles with the best observation likelihood are shown in the figures. Similar as in the previous section, we did a repeatability test, i.e., we tracked the objects over ten independent runs. The tracked objects are initialized by hand in the very first frame.

Fig. 14 shows the average standard deviation of the trajectories of ten tracking runs using a learning rate α in the range of 0, . . . , 0.6. The optimal learning rate for the *Kid* and the *Adult* is $\alpha = 0.1$ and $\alpha = 0.2$, respectively. Currently, α is fixed for the whole image sequence. Ideally, α could be adapted depending on the dynamics of the scene.

623

V. CONCLUSION

We propose a robust visual tracking algorithm for multiple objects (faces of people) in a meeting scenario based on low-level features as skin color, target motion, and target size. Based on these features, automatic initialization and termination of objects is performed. For tracking a sampling importance resampling, particle filter has been used to propagate sample distributions over time. Furthermore, we use online learning of the target models to handle the appearance variability of the objects. We discuss the similarity between our implemented tracker and GAs. Each particle represents an individual in the GA framework. The evaluation function incorporates the observation likelihood model and the individual selection

process maps to the resampling procedure in the particle filter. The state-space dynamics is incorporated in the recombination and mutation operator of the GA. Numerous experiments on meeting data show the capabilities of the tracking approach. The participants were successfully tracked over long image sequences. Partial occlusions are handled by the algorithm. Additionally, we empirically show that the adaptation of the reference model during tracking of indoor and outdoor scenes results in a more robust tracking.

Future work concentrates on extending the tracker to other scenarios and to investigate an adaptive reference model learning rate α which depends on the dynamics of the scene. Furthermore, we aim to develop approaches for tackling occlusions.

ACKNOWLEDGMENT

This work was supported by the Austrian Science Fund (Project S106). The author would like to thank M. Grabner and M. Kepesi who collected the data during their involvement in the MISTRAL Project (www.mistral-project.at). The MISTRAL Project was funded by the Austrian Research Promotion Agency (www.ffg.at) within the strategic objective FIT-IT under Project 809264/9338. The author would also like to thank C. Kirchstätter for recording the indoor and outdoor video.

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